

# **Forbidden Pitch or Duty-Free Revealing the Causes of Across- Pitch Imaging Differences**

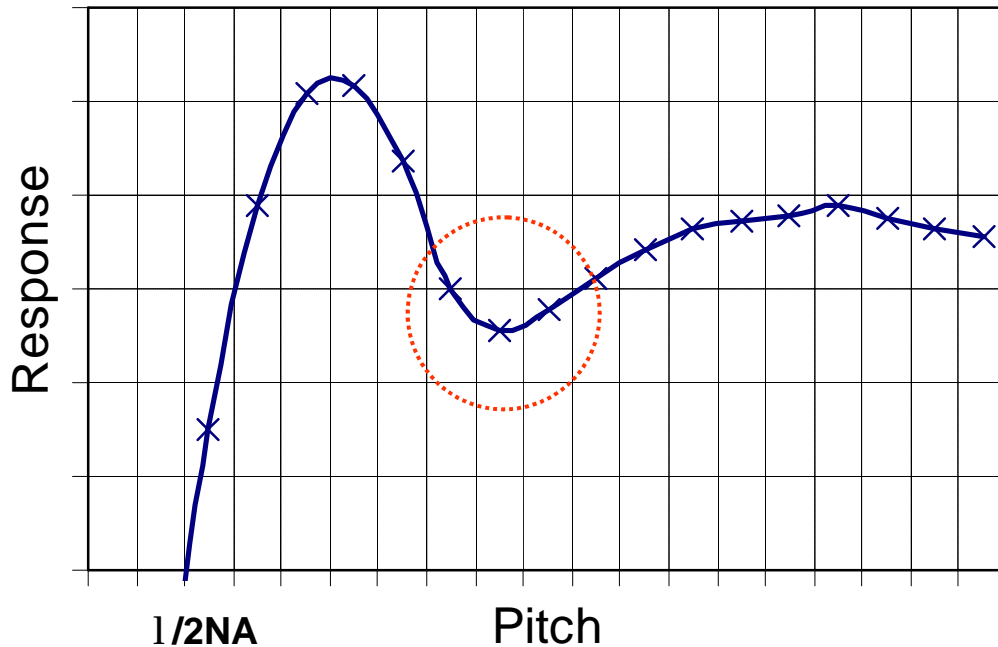
**Bruce W. Smith**

**Rochester Institute of Technology**



# Forbidden or Problematic

Nothing is forbidden <sup>3</sup>  $1/2NA$



- Response may be CD, placement error, modulation, NILS, profile, etc.
- “Forbidden” is a message for designers.
- Lithographers don't like to be told what to do.
- Sensitivities should not provide excuses.
- Nothing forbidden  $> 1/2NA$ .

# Imaging Situations

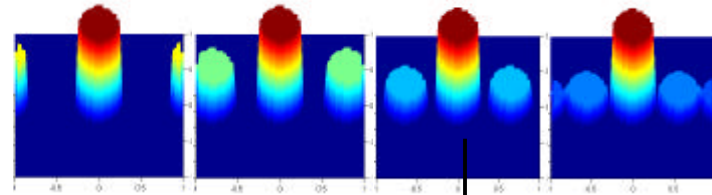
1. **Binary masking effects**
2. **Off-axis illumination effects**
3. **Assist feature effects**
4. **Contact side-lobes**
5. **Aberration effects**



# CD Variation with Pitch

## Conventional Binary Masking

CD variation is a consequence of order capture and diffraction energy



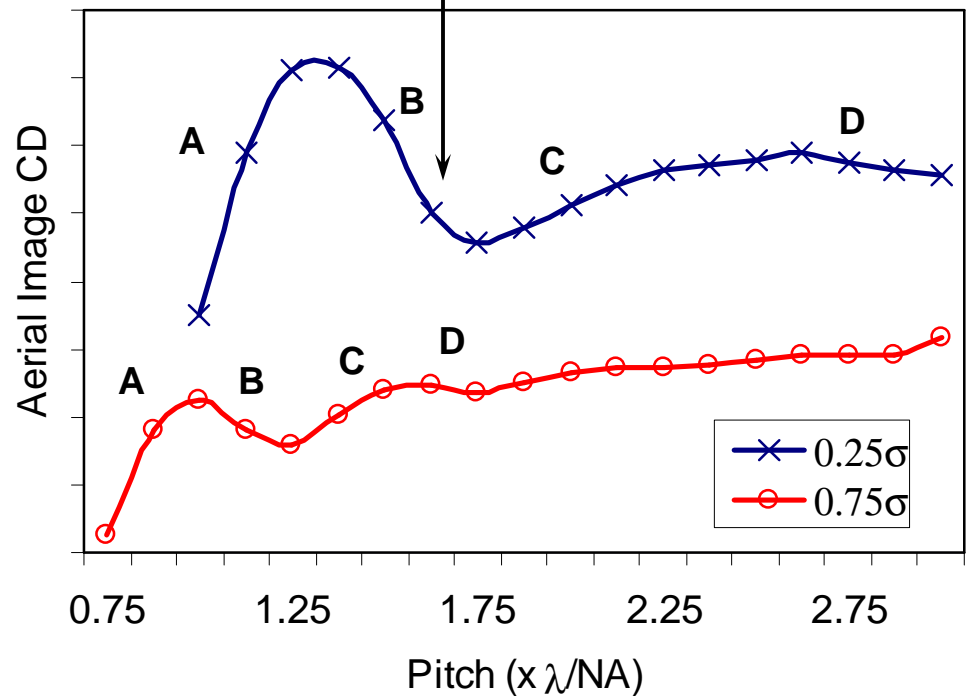
### Dominant Effect

A - 1<sup>st</sup> order capture  $\frac{l}{(s+1)NA}$

B - Zero order increase  $\frac{l}{(s-1)NA}$

C - 2<sup>nd</sup> order capture  $\frac{2l}{(s+1)NA}$

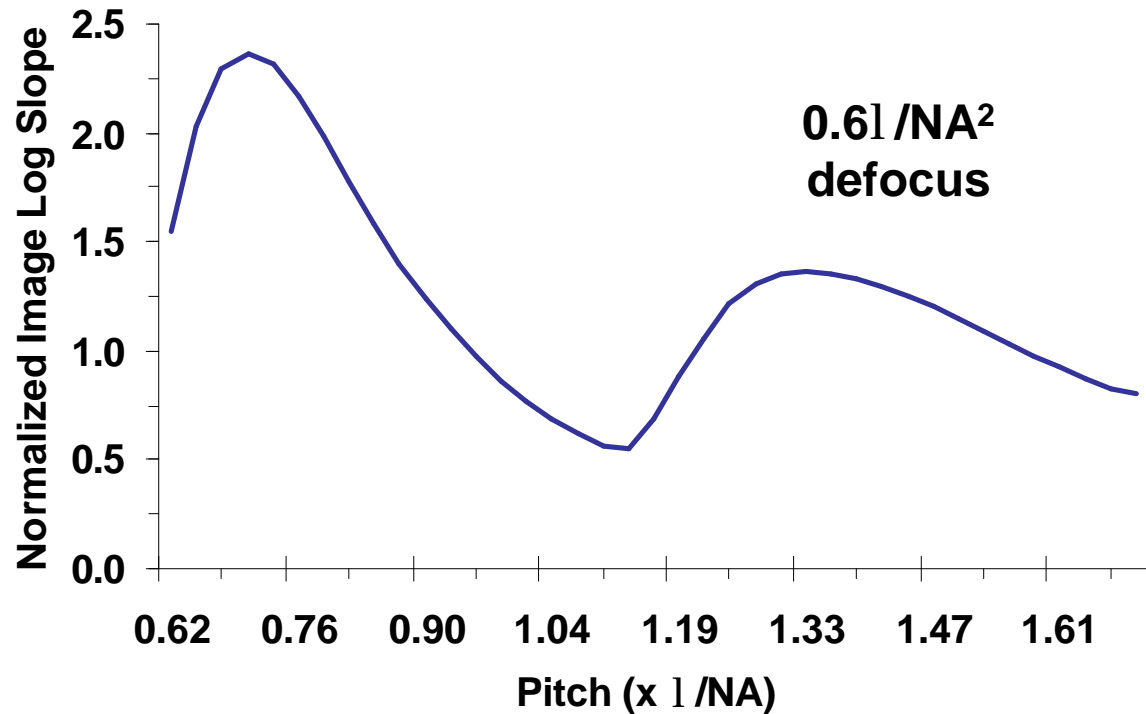
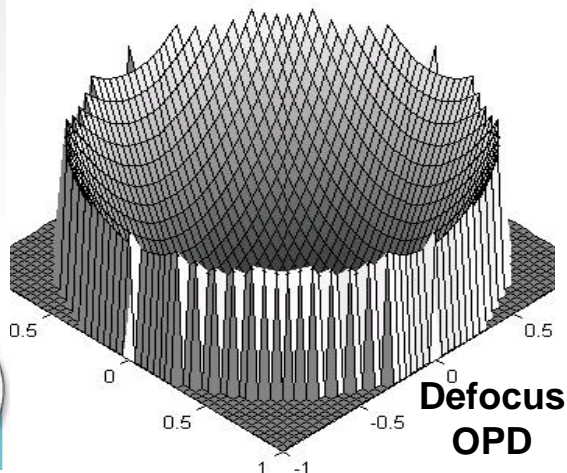
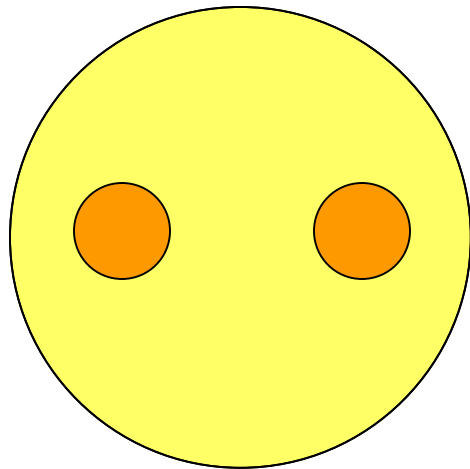
D - Zero order increase  $\frac{2l}{(s-1)NA}$



# Illumination and Problematic Pitch

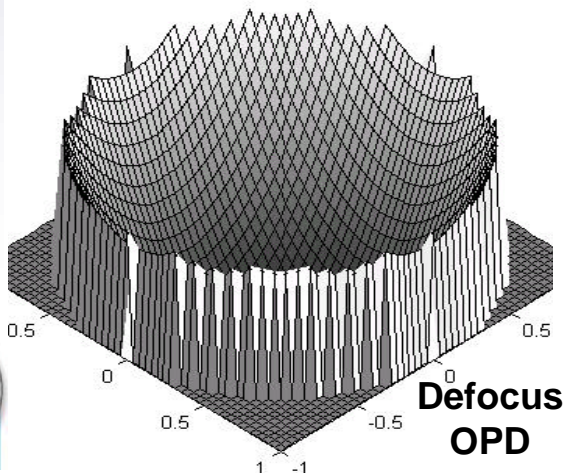
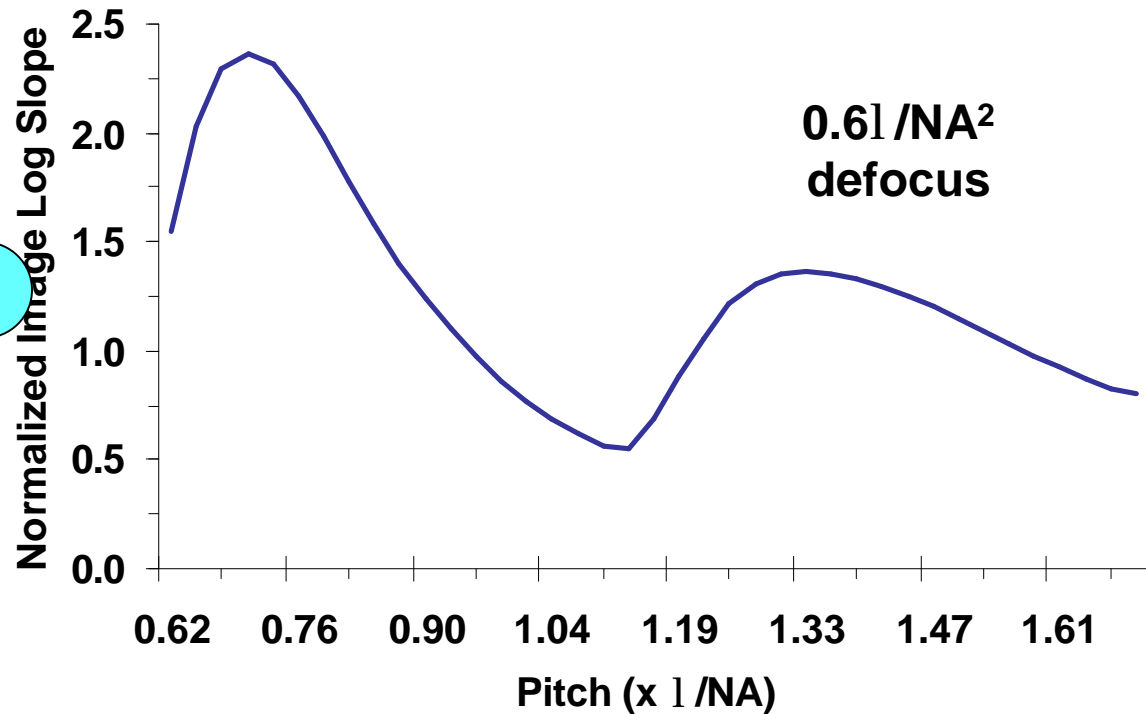
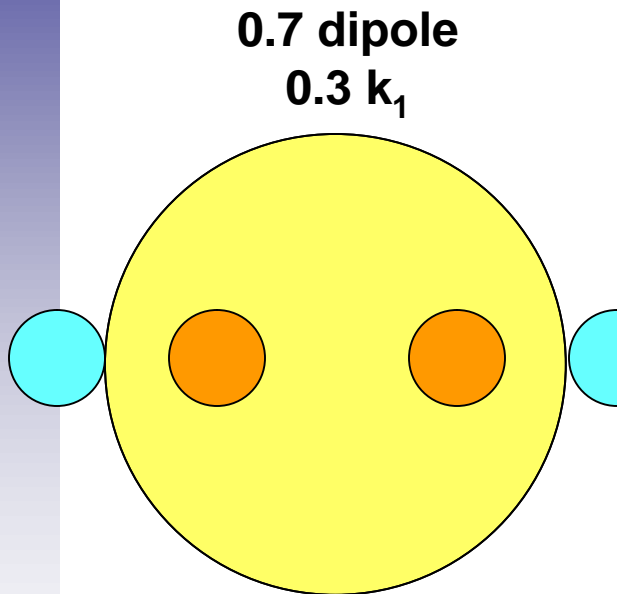
OAI for one pitch can be worst case for another

0.7 dipole



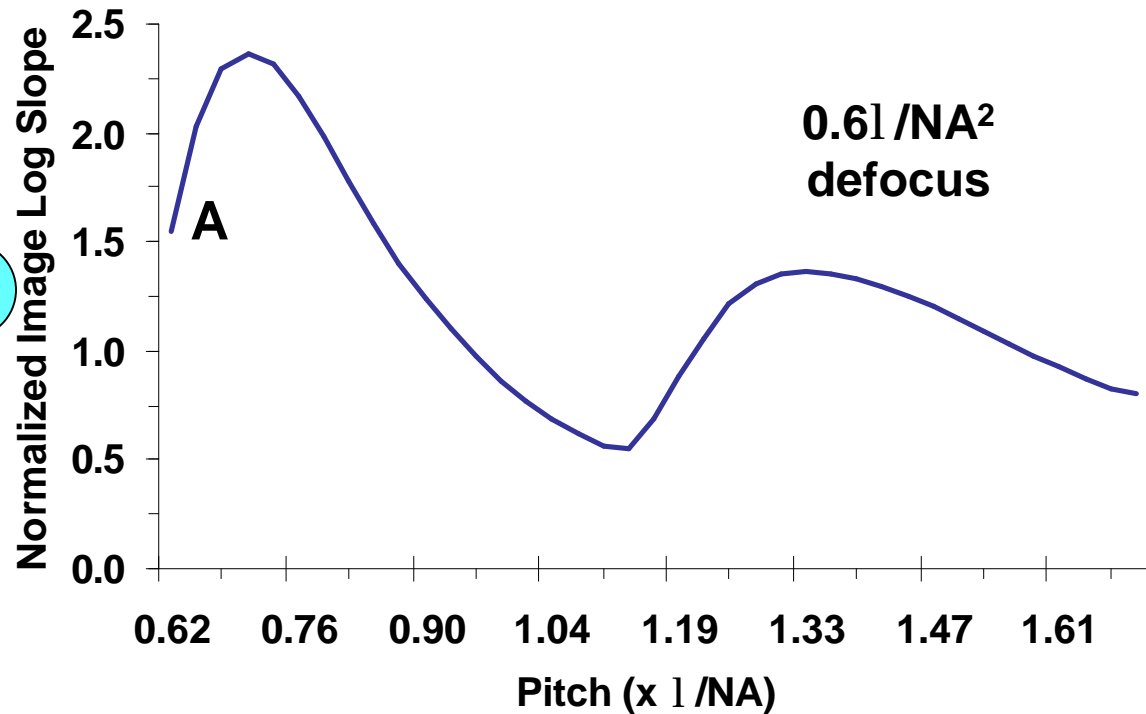
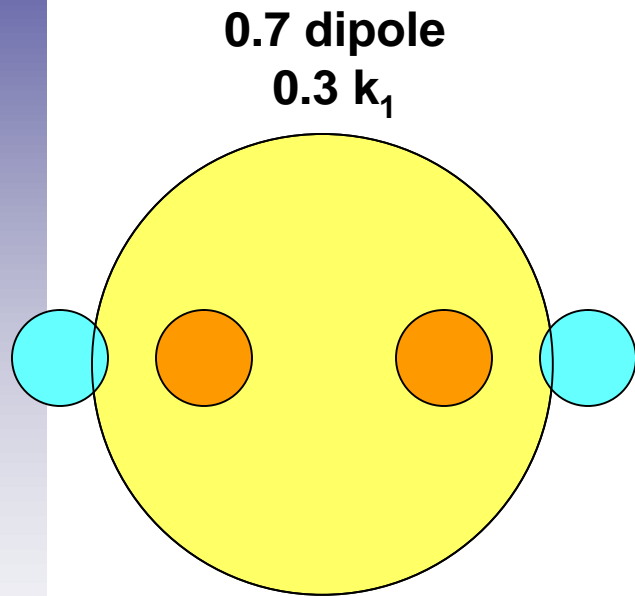
# Illumination and Problematic Pitch

OAI for one pitch can be worst case for another

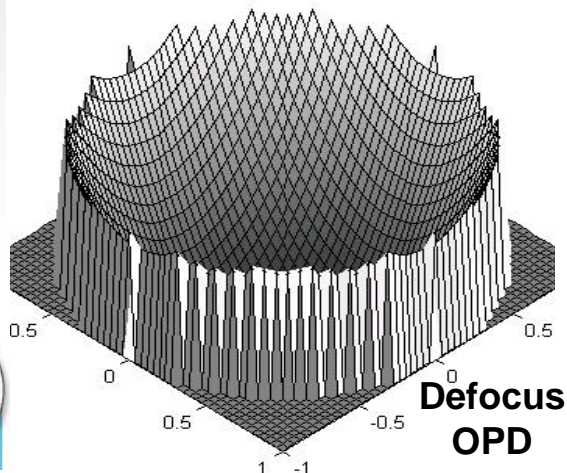


# Illumination and Problematic Pitch

OAI for one pitch can be worst case for another

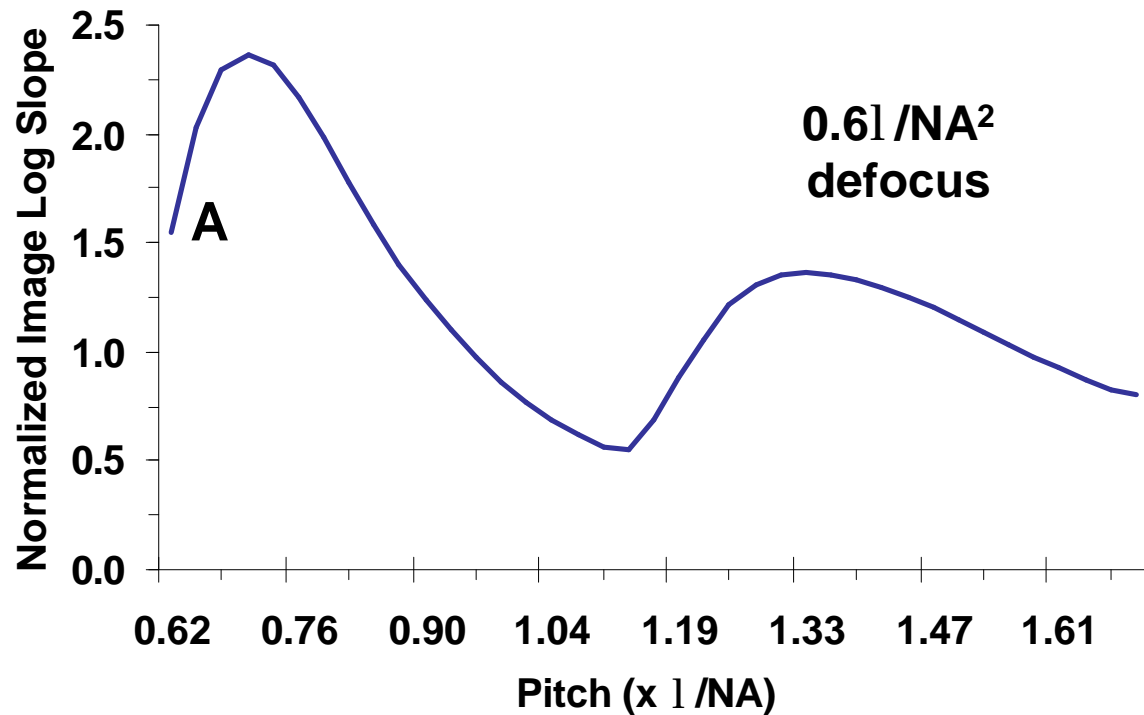
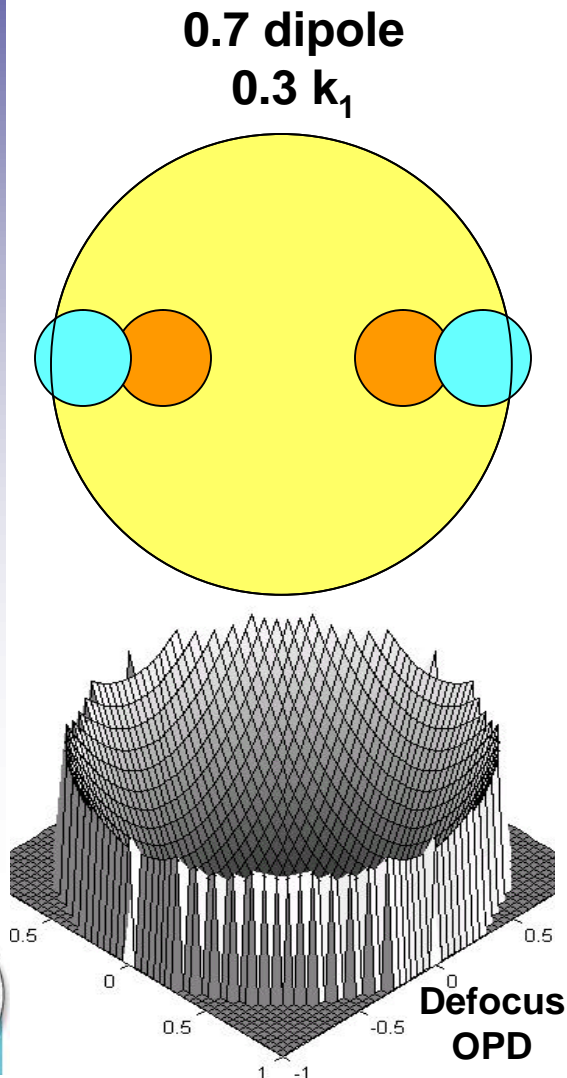


A - 1<sup>st</sup> order capture



# Illumination and Problematic Pitch

OAI for one pitch can be worst case for another



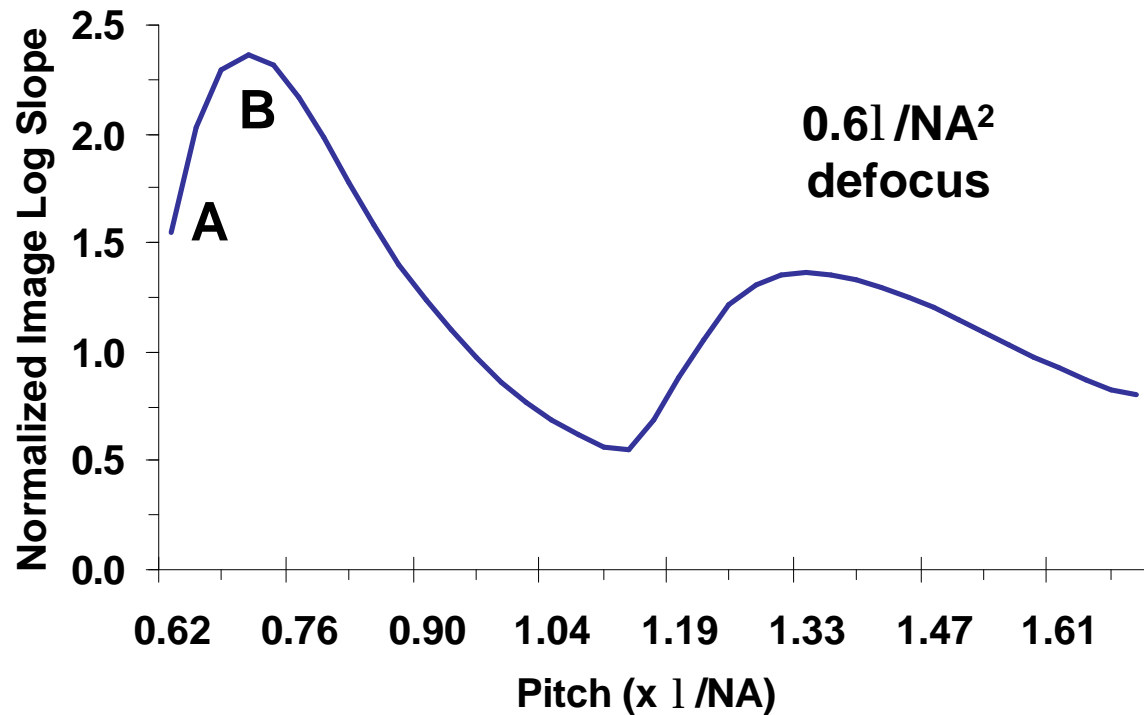
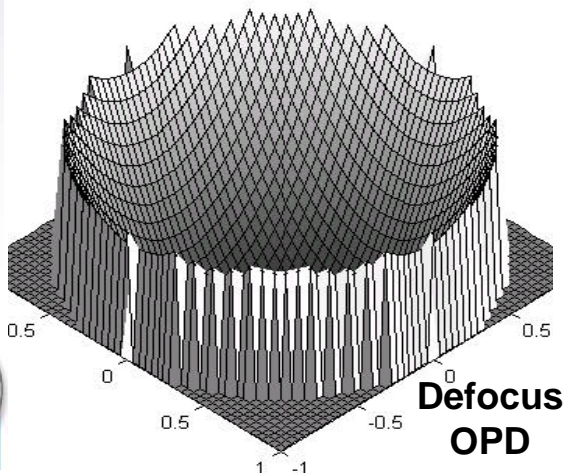
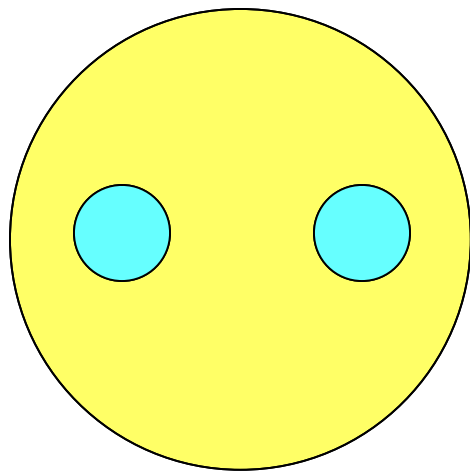
A - 1<sup>st</sup> order capture



# Illumination and Problematic Pitch

OAI for one pitch can be worst case for another

0.7 dipole  
0.3  $k_1$



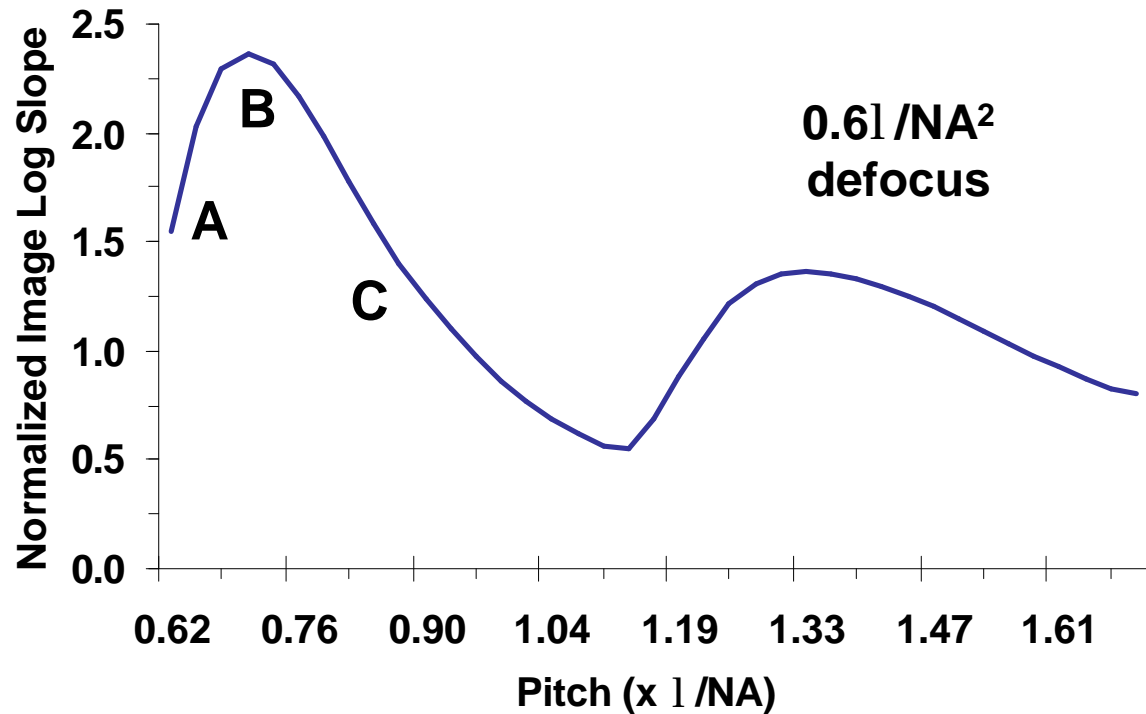
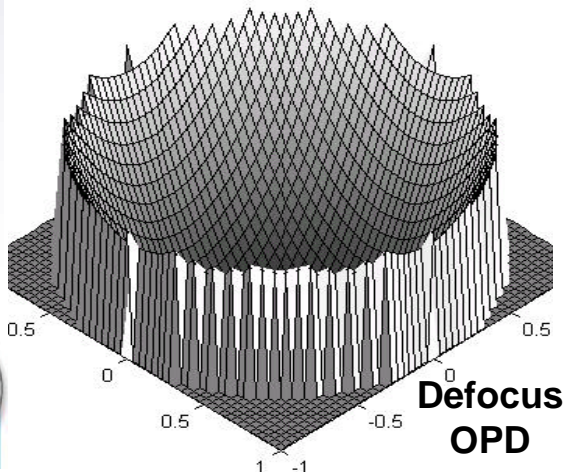
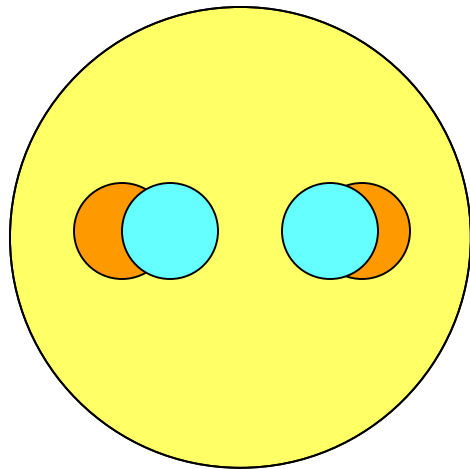
A - 1<sup>st</sup> order capture

B - 0<sup>th</sup> and 1<sup>st</sup> overlap

# Illumination and Problematic Pitch

OAI for one pitch can be worst case for another

0.7 dipole  
0.3  $k_1$



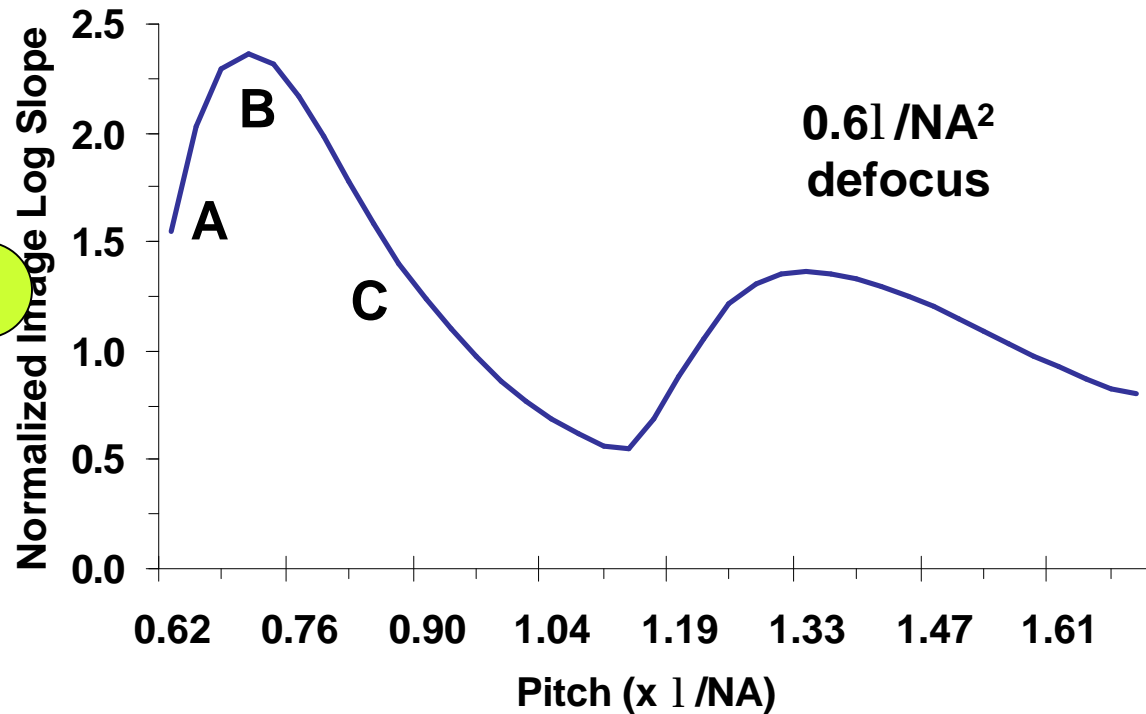
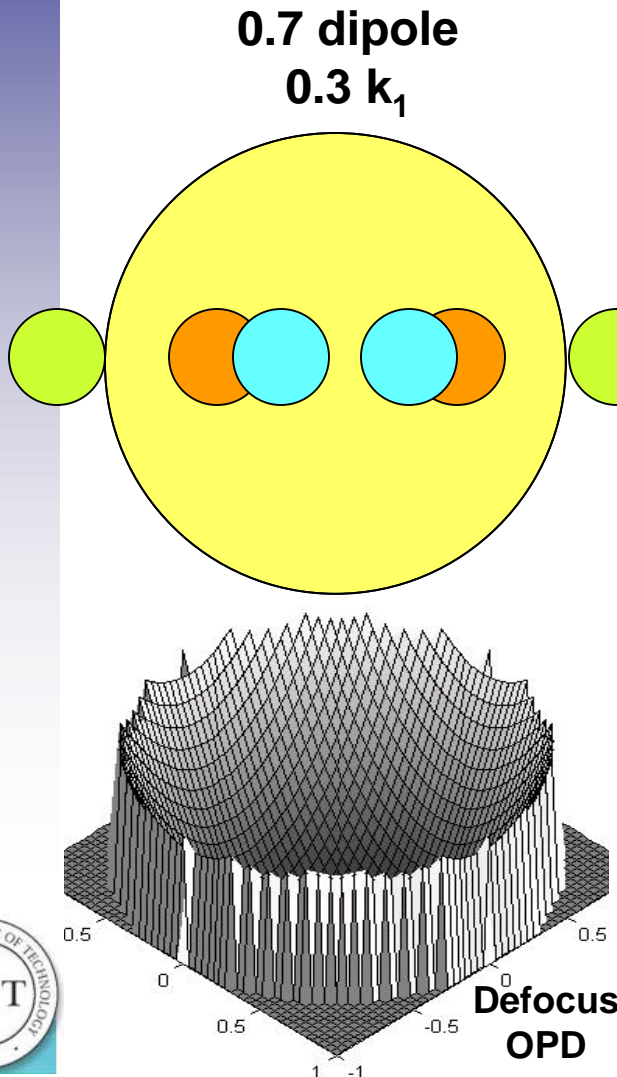
A - 1<sup>st</sup> order capture

B - 0<sup>th</sup> and 1<sup>st</sup> overlap

C - 1<sup>st</sup> into center

# Illumination and Problematic Pitch

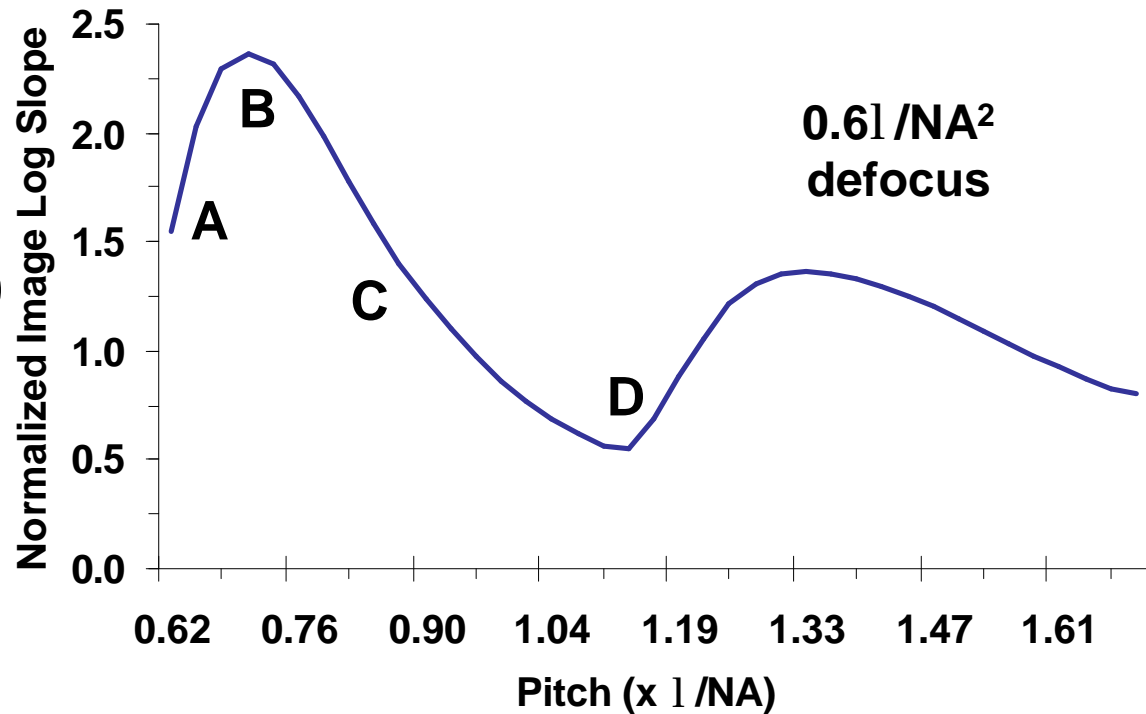
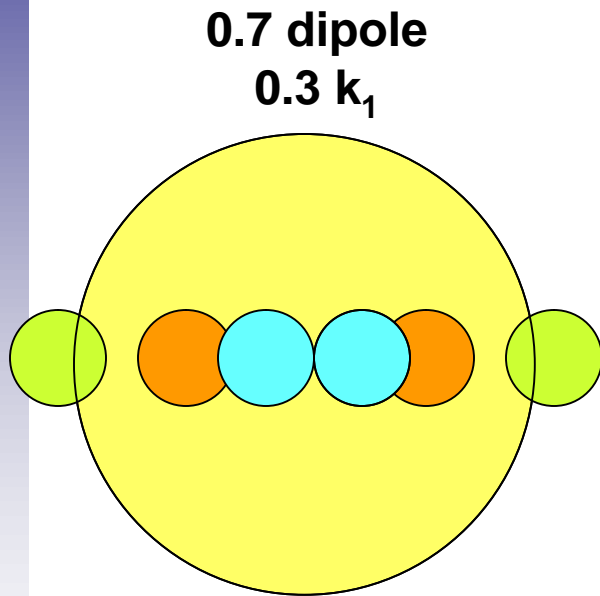
OAI for one pitch can be worst case for another



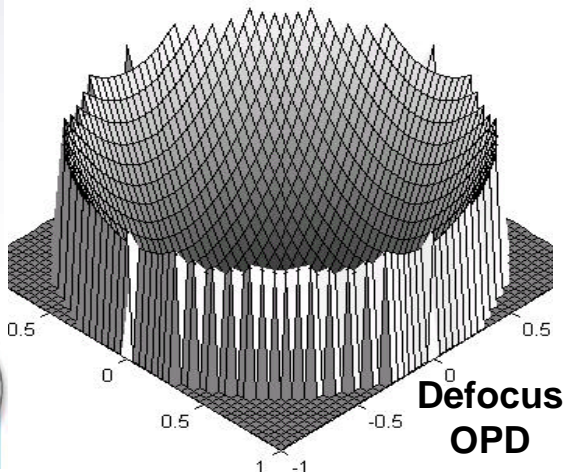
- A - 1<sup>st</sup> order capture
- B - 0<sup>th</sup> and 1<sup>st</sup> overlap
- C - 1<sup>st</sup> into center
- D - 2<sup>nd</sup> order capture

# Illumination and Problematic Pitch

OAI for one pitch can be worst case for another



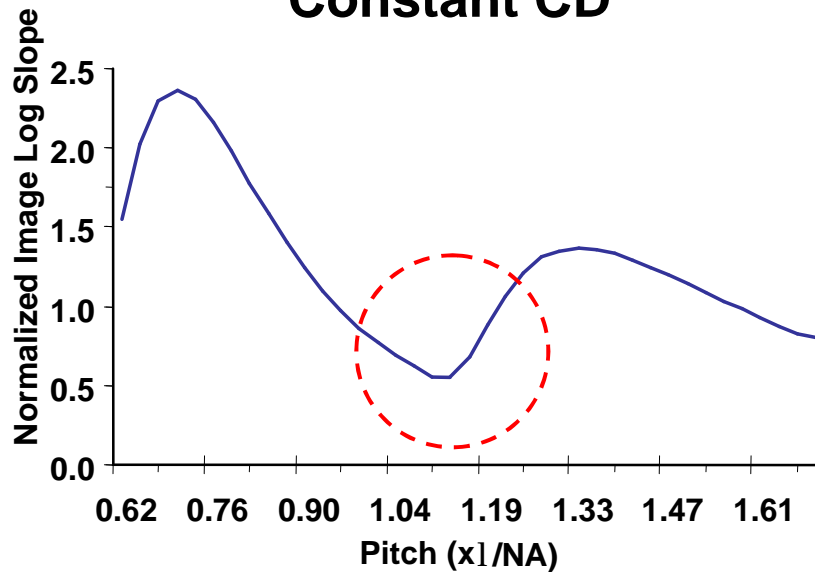
- A - 1<sup>st</sup> order capture
- B - 0<sup>th</sup> and 1<sup>st</sup> overlap
- C - 1<sup>st</sup> into center
- D - 2<sup>nd</sup> order capture



# Illumination and Problematic Pitch

## The second order effect

Increasing pitch  
Constant CD



Increasing pitch  
1:1 ratio

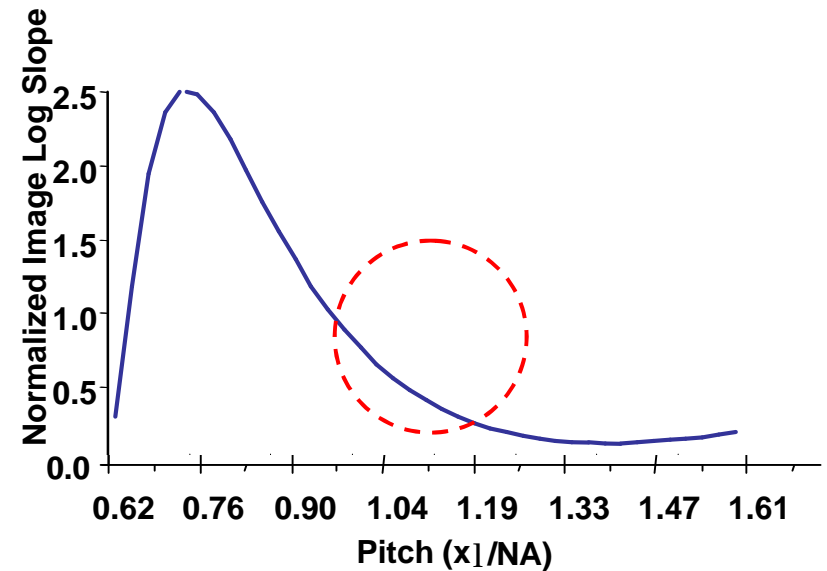
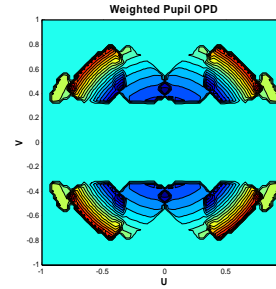
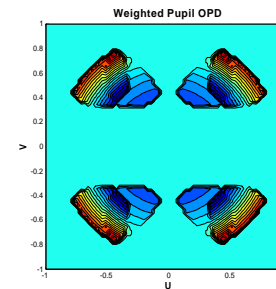
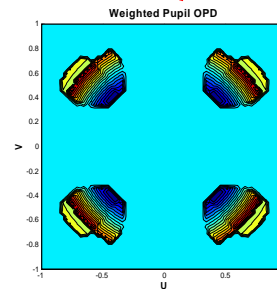
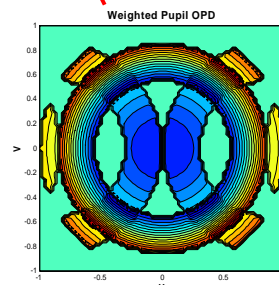
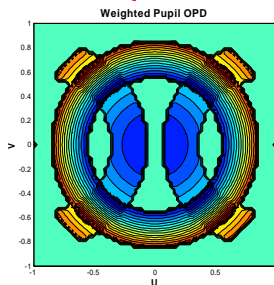
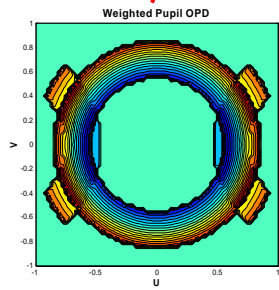
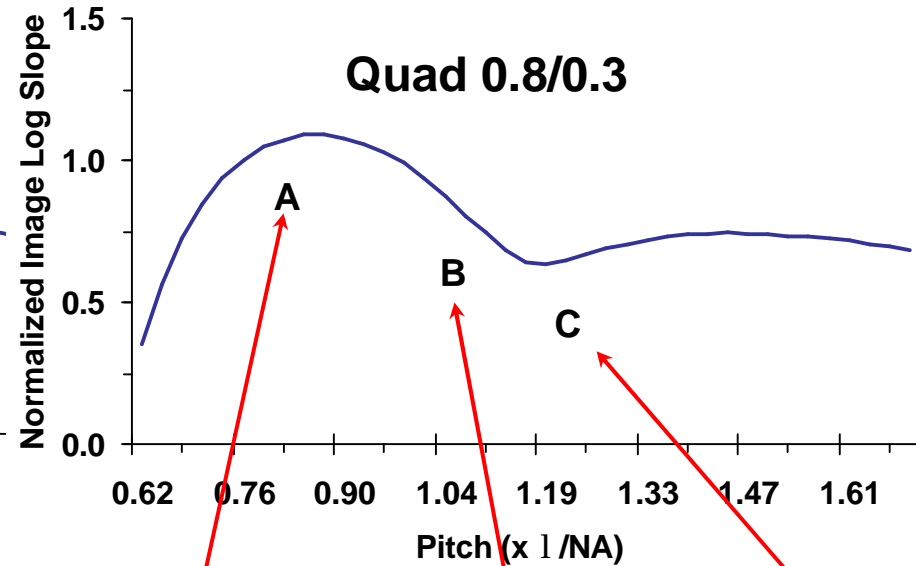
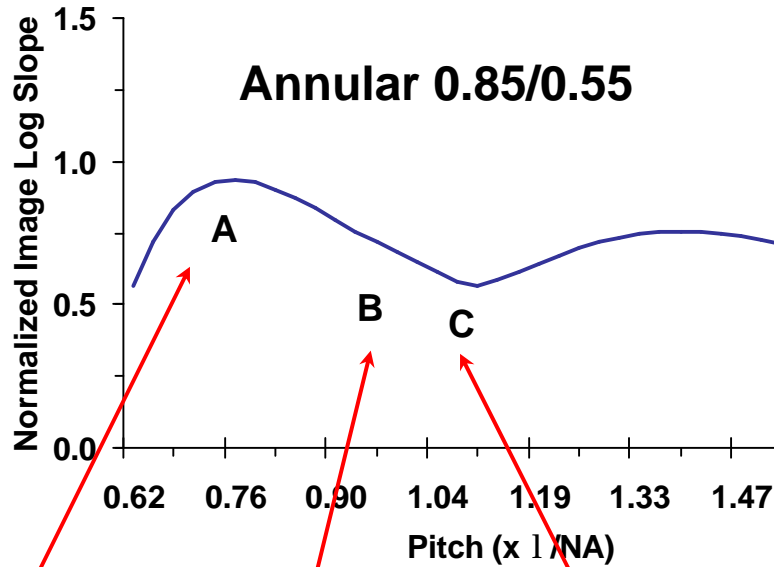


Image quality continues to decrease until the 3<sup>rd</sup> order is collected.

# Illumination and Problematic Pitch

## Annular and Quadrupole Illumination



**A – 0<sup>th</sup> and 1<sup>st</sup> overlap**

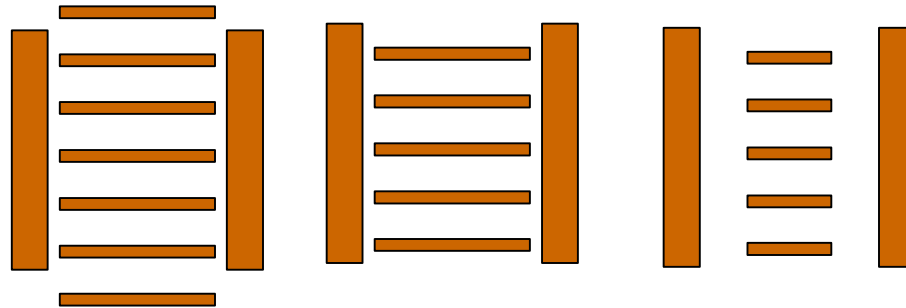
**B – 1<sup>st</sup> into center**

**C – 2<sup>nd</sup> order capture**

# Assist Feature OPC

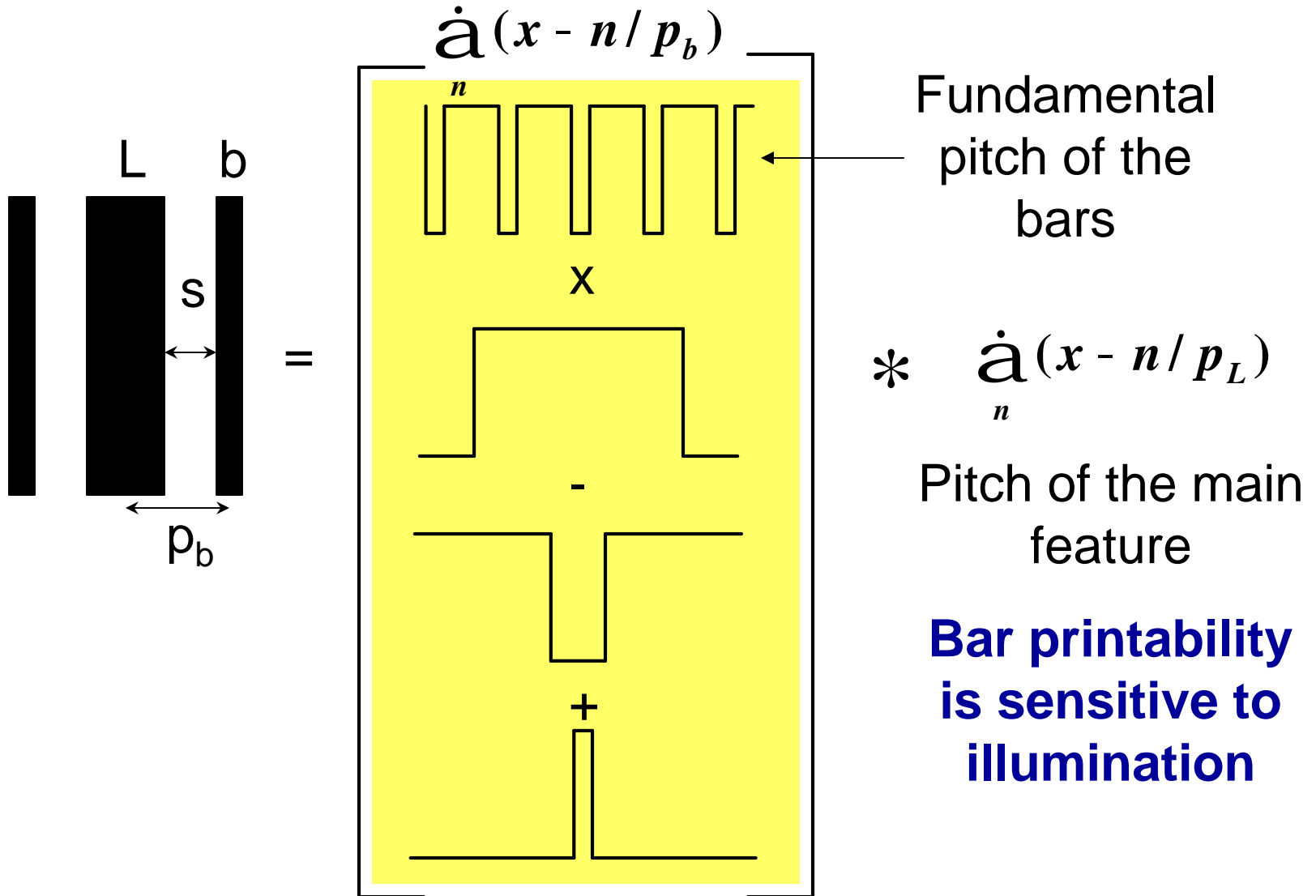
- Assist features are subjected to the same illumination considerations as main feature.
- Assist features will print at problematic pitch harmonics
- Orientation of bars can help, especially with OAI.

No problematic pitch with dipole.



# One pair of bars

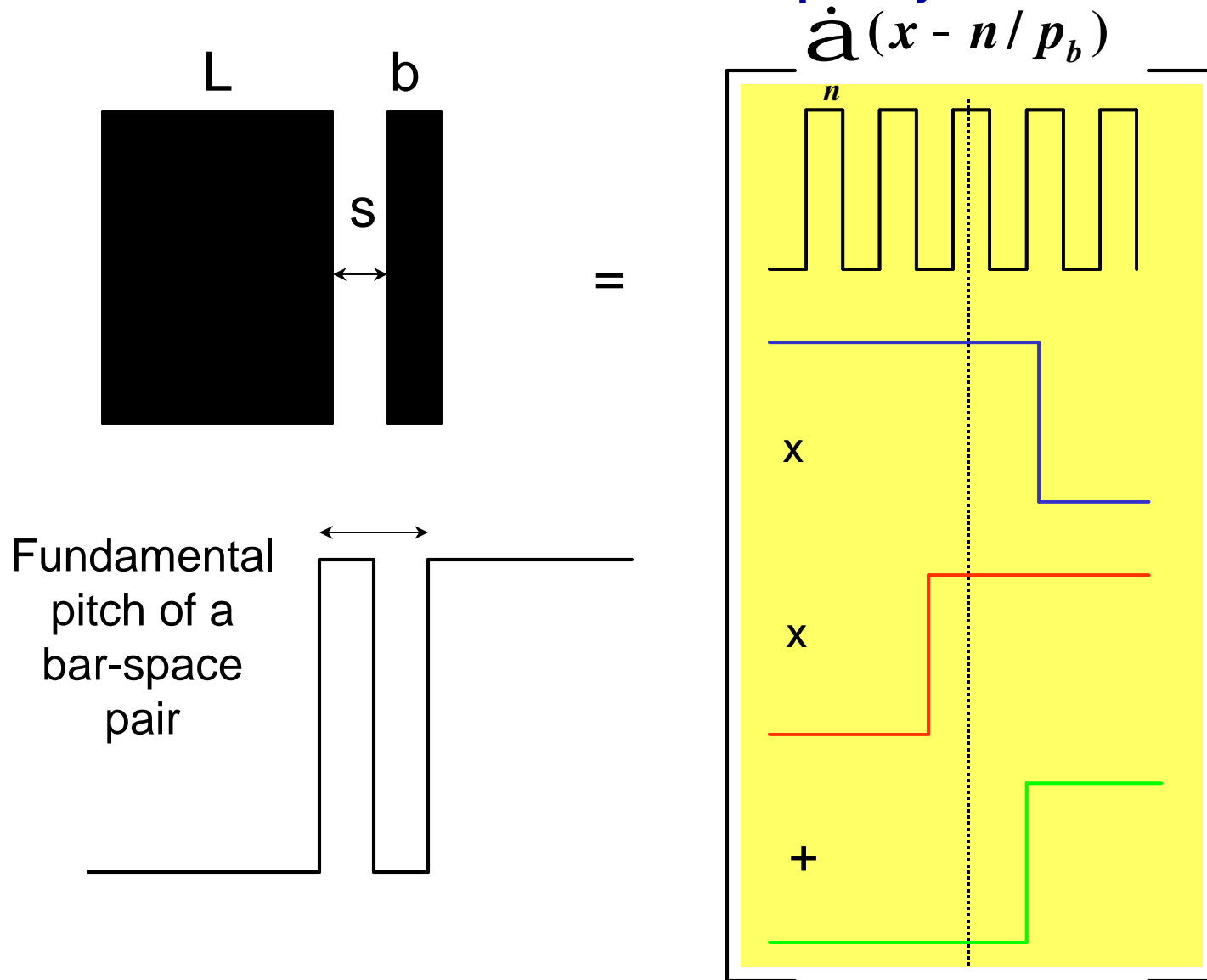
Consideration of main feature and bar pitch





# The (bar + space) effect only

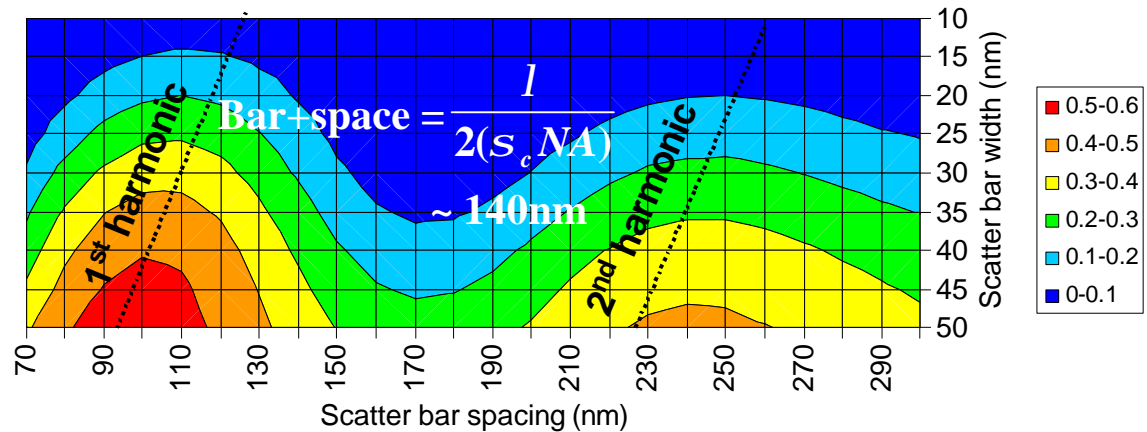
Is there a “hidden frequency”?



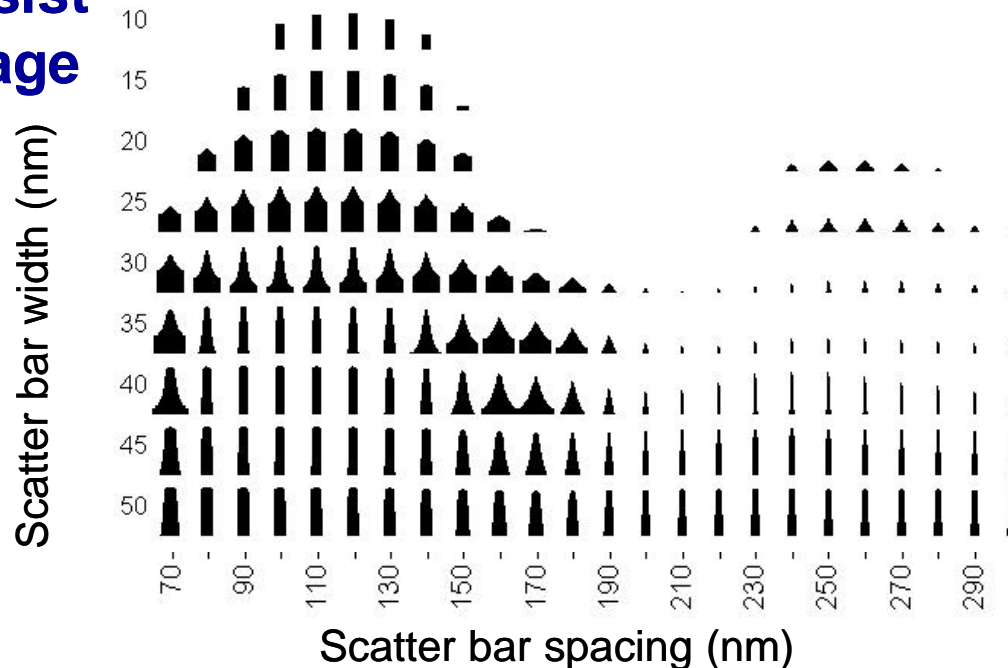
# Printability of (bar + space) combinations

193nm/0.8NA/0.65-0.95 annular/ 70nm semi-iso CD

Aerial  
Image  
Contrast



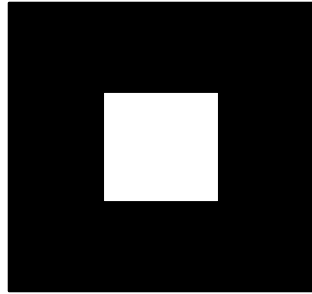
Resist  
Image



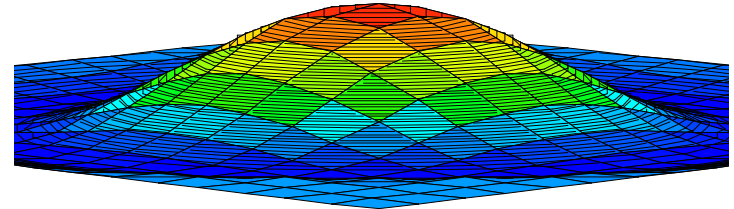
# Contacts and Sidelobes

## The Contact Misconception

Drawn  
contact



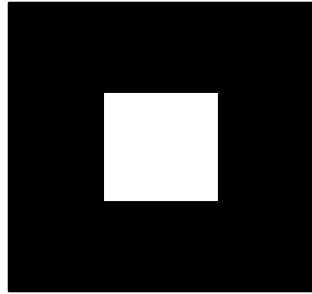
Diffraction



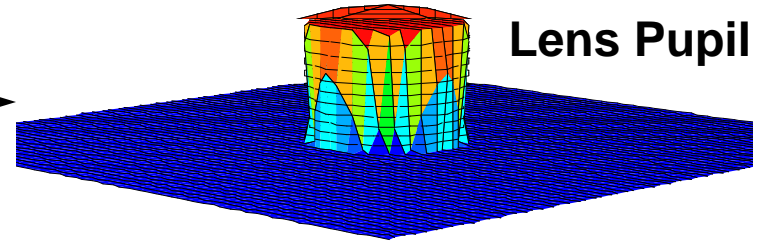
# Contacts and Sidelobes

## The Contact Misconception

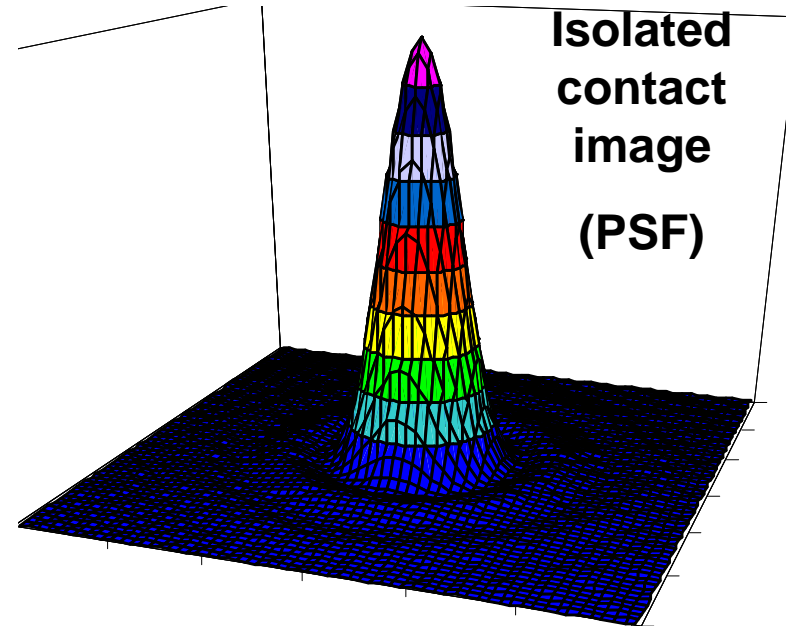
Drawn  
contact



Diffraction



Lens Pupil

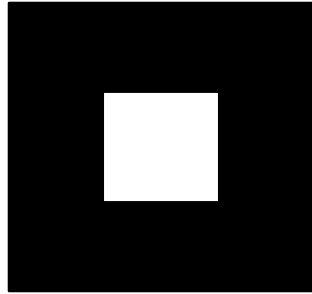


Isolated  
contact  
image  
(PSF)

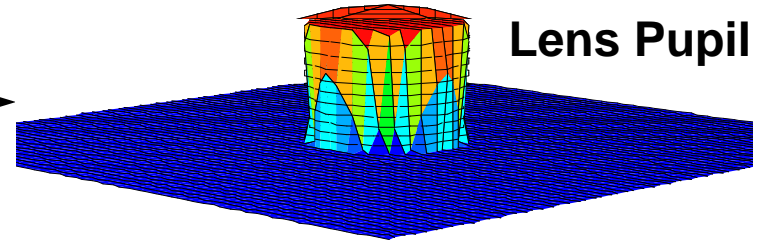
# Contacts and Sidelobes

## The Contact Misconception

Drawn  
contact

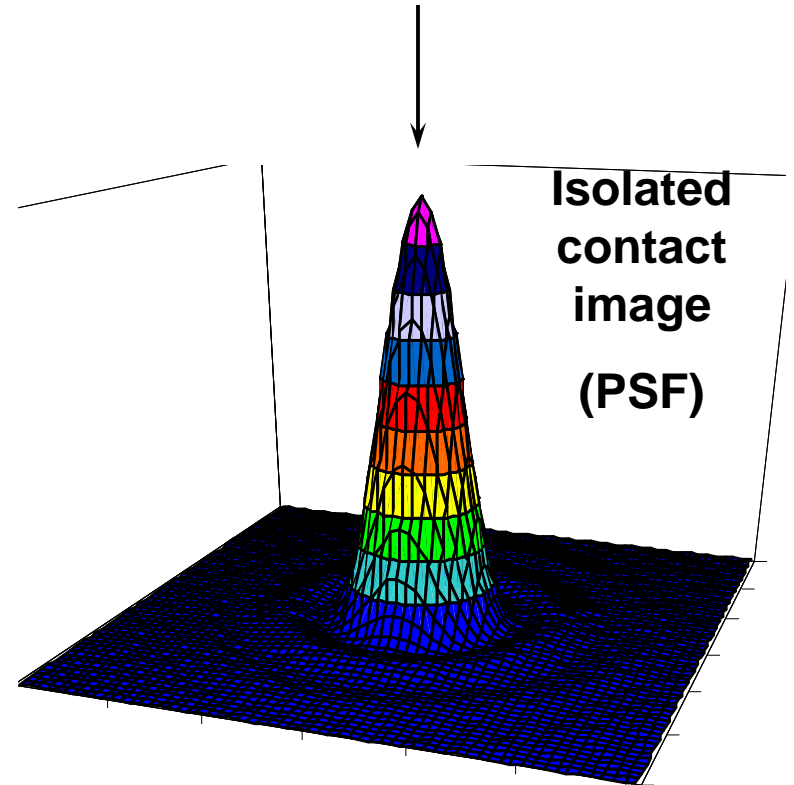


Diffraction

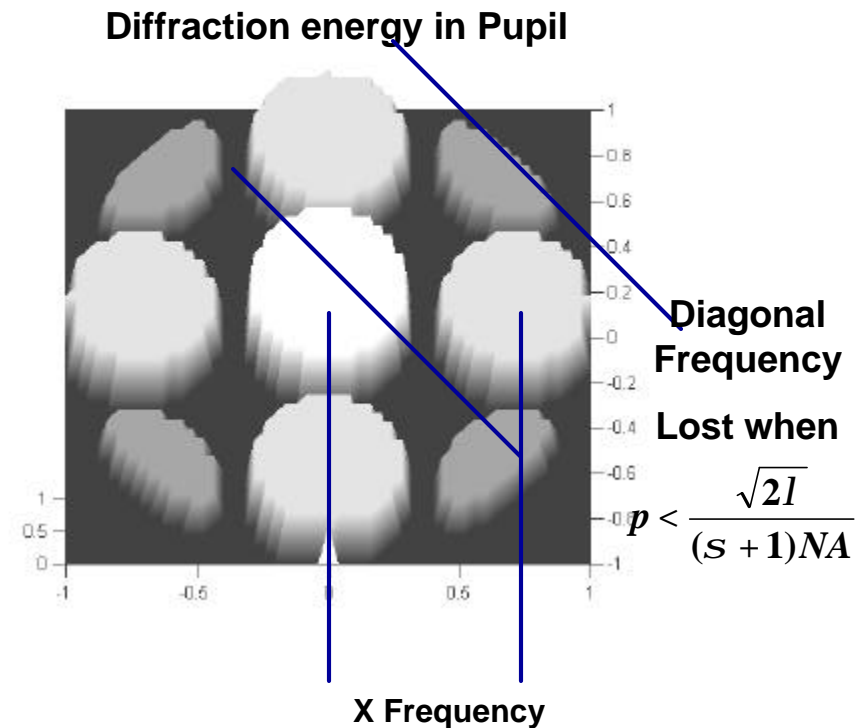
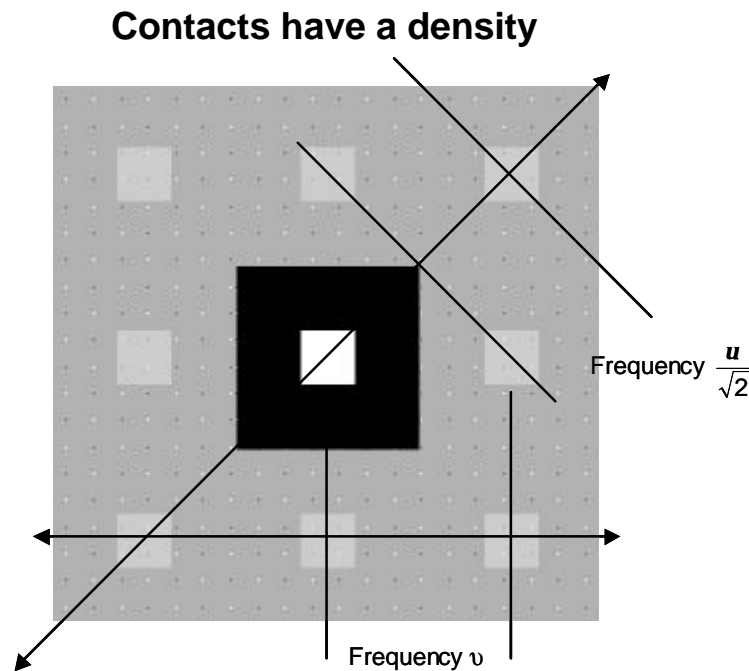


### The Contact Reality

1.  $\text{Besinc}^2$  lobes only for isolated contacts.
2. “Gibb’s Phenomenon” only for Fourier Series with orders  $> 1$ .



# Contact Frequency and Sidelobes



$$|\text{Mag.}|_{\text{zero order}} = (s/p)$$

$$|\text{Mag.}|_{\text{first order}} = \left| \left( \frac{s}{p} \right) \text{sinc} \left( \frac{s}{p} \right) \right|$$

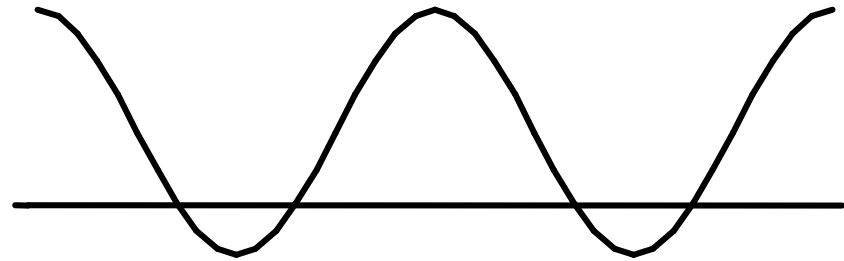
# Coherent 1:2 Contact Image

Capture of 0, +/- 1 orders – biased cosine

Contact Image =  
 $|\text{zero order} + \text{first order cosine}|^2$

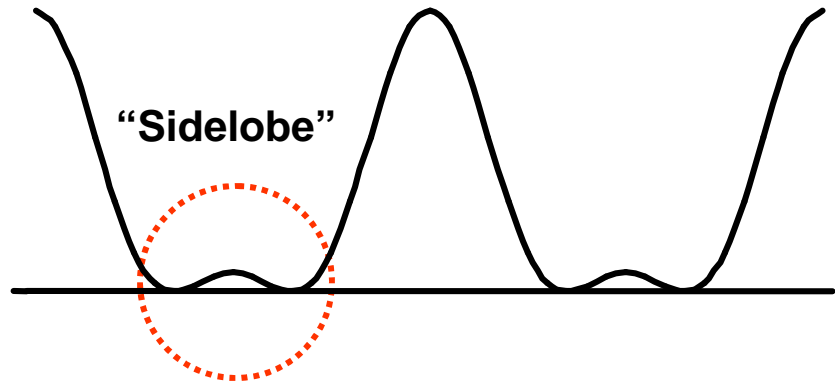
$$0.33 + 0.56\cos(2\pi u_0 x)$$

Image Amplitude



$$(0.33 + 0.56\cos(2\pi u_0 x))^2$$

Image Intensity



# Images with decreasing pitch

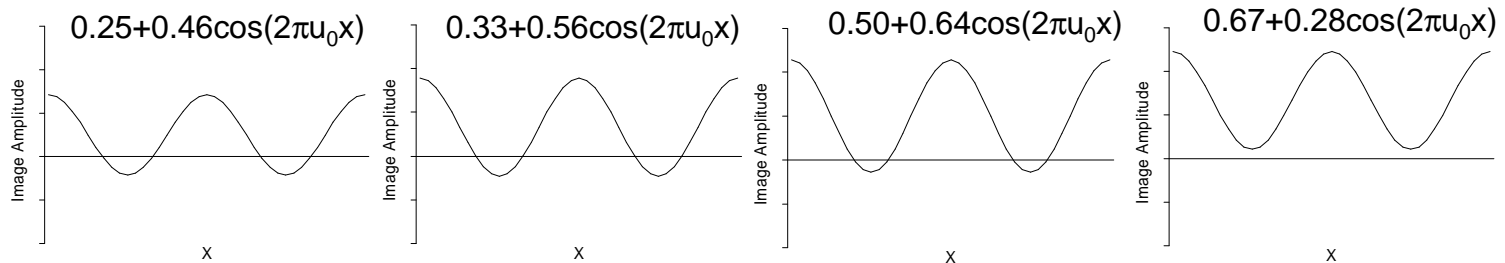
1:3 contacts

1:2 contacts

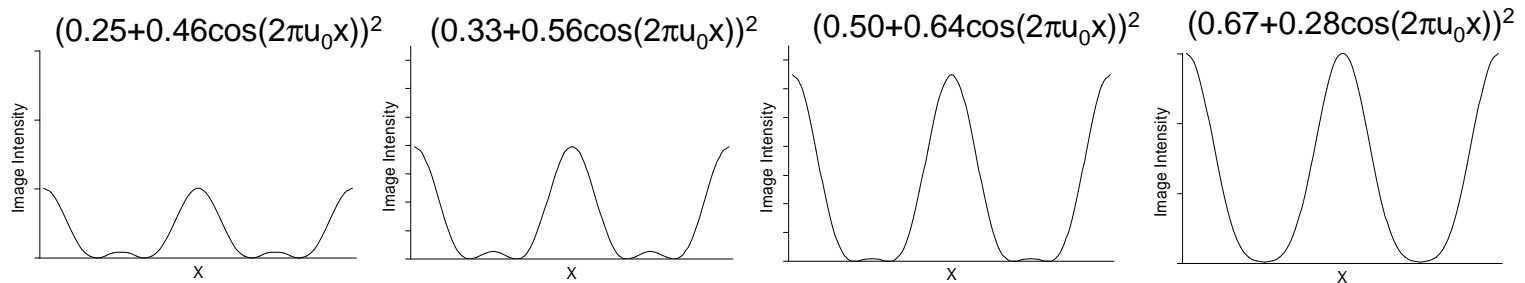
1:1 contacts

2:1 contacts

Amplitude



Intensity



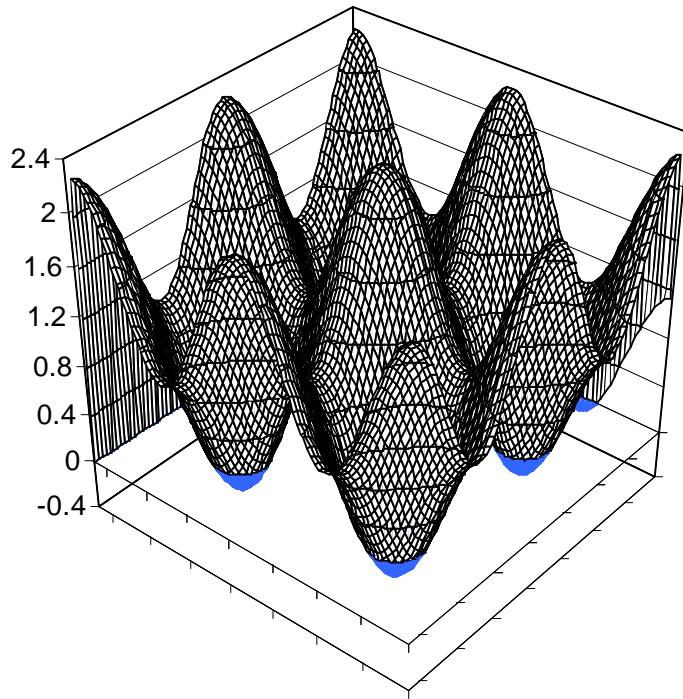
**Both lobes of the 1<sup>st</sup> order cosine may print!**



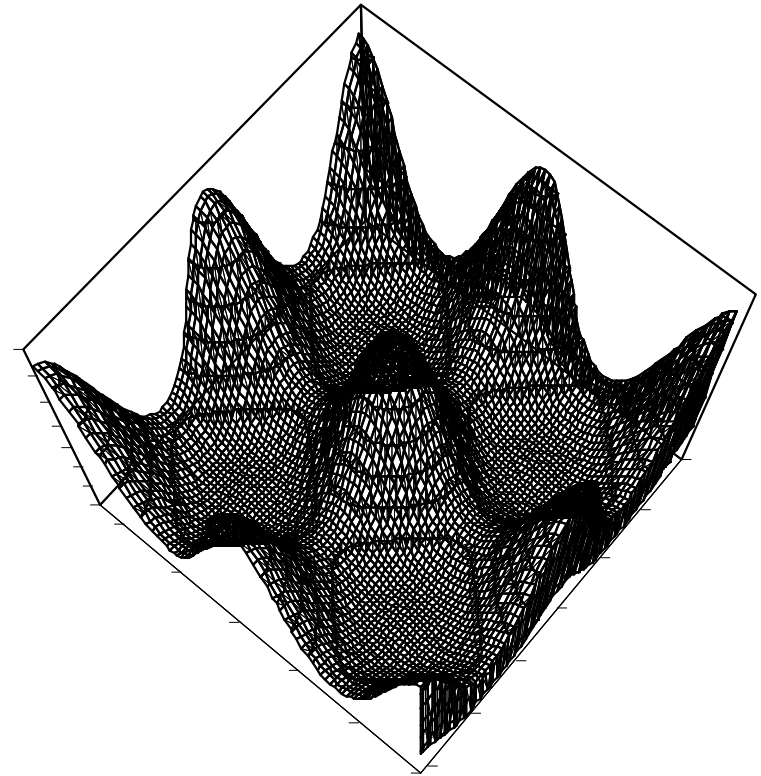
# Contacts on 2D

## X/Y Sum of Biased Cosines

1:1



**Amplitude**

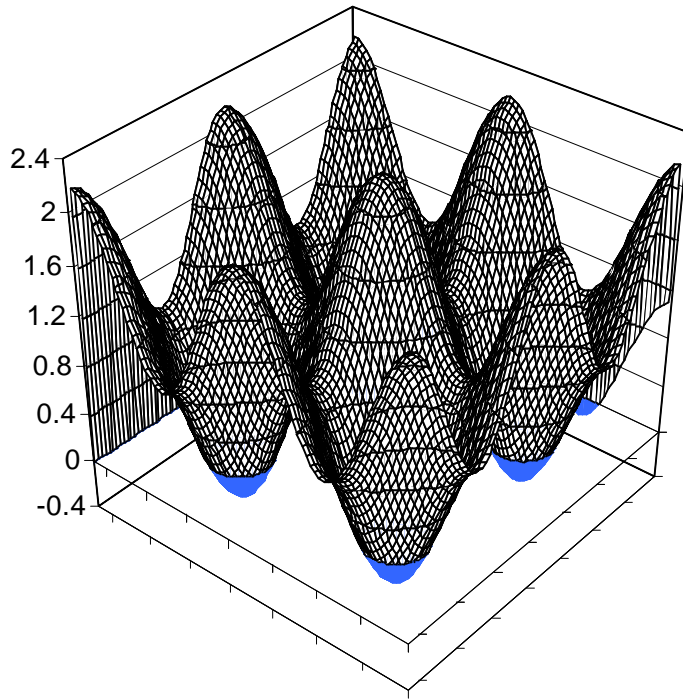


**Intensity**

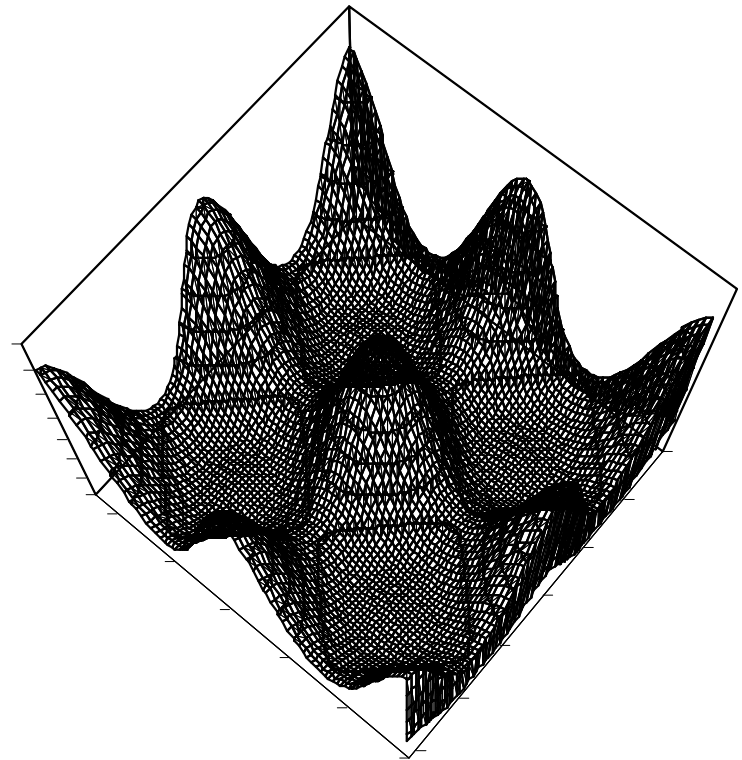
# Contacts on 2D

## X/Y Sum of Biased Cosines

1:1.2



**Amplitude**

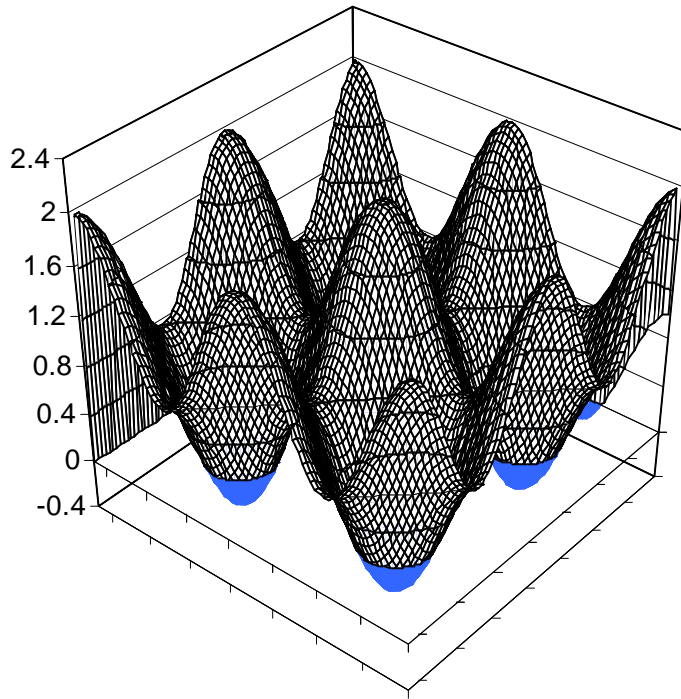


**Intensity**

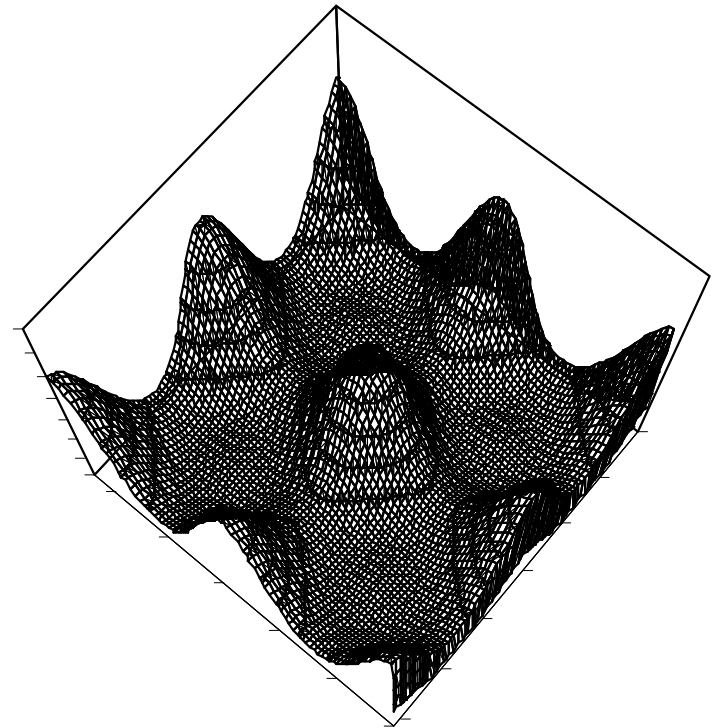
# Contacts on 2D

## X/Y Sum of Biased Cosines

1:1.5



**Amplitude**

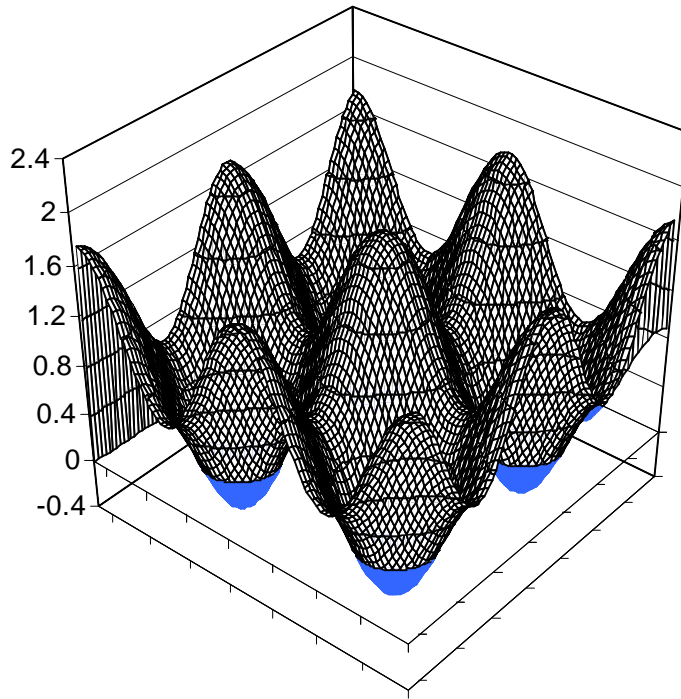


**Intensity**

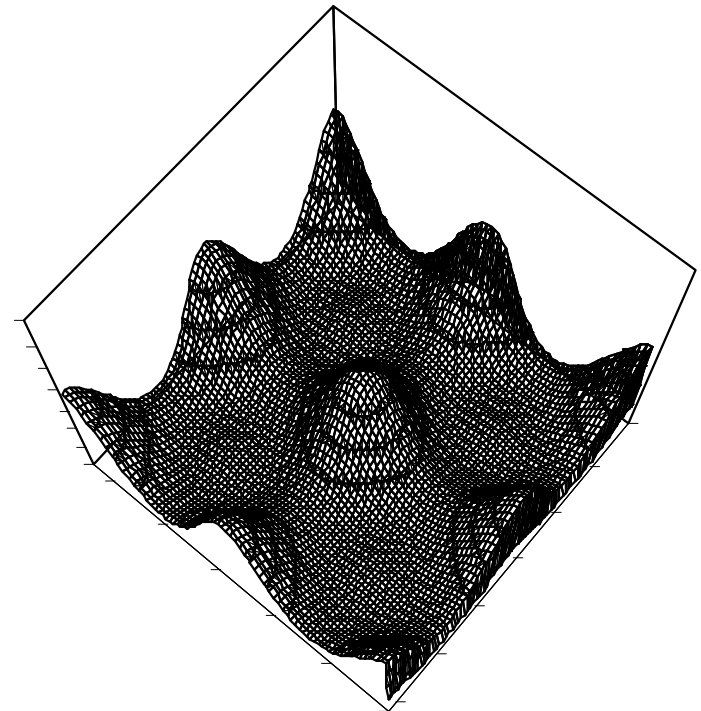
# Contacts on 2D

## X/Y Sum of Biased Cosines

1:2



**Amplitude**

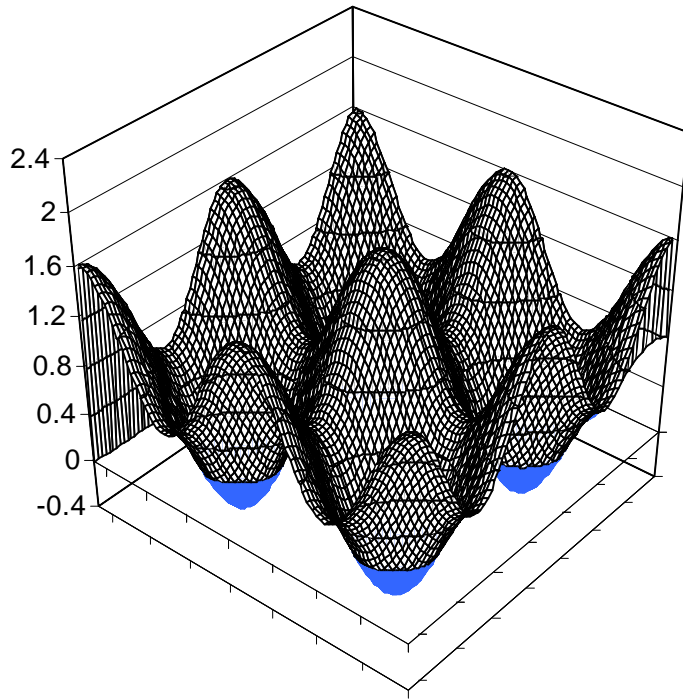


**Intensity**

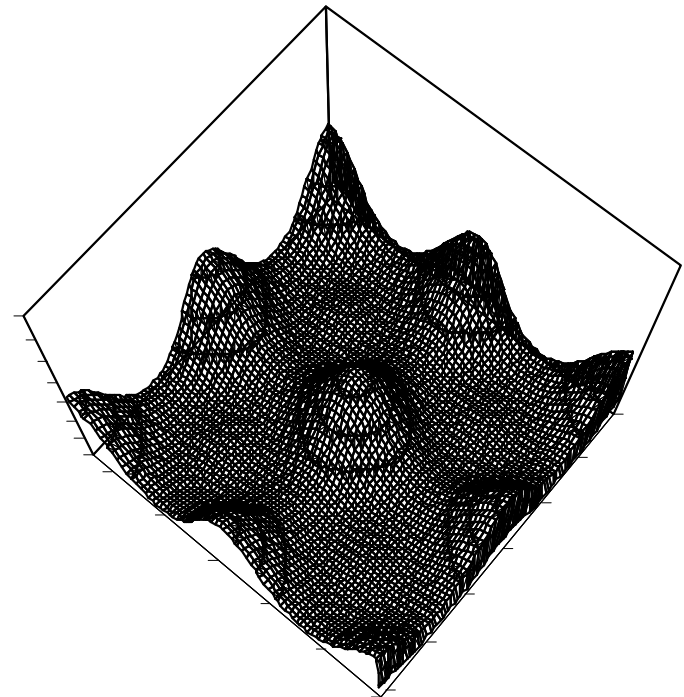
# Contacts on 2D

## X/Y Sum of Biased Cosines

1:2.5



**Amplitude**

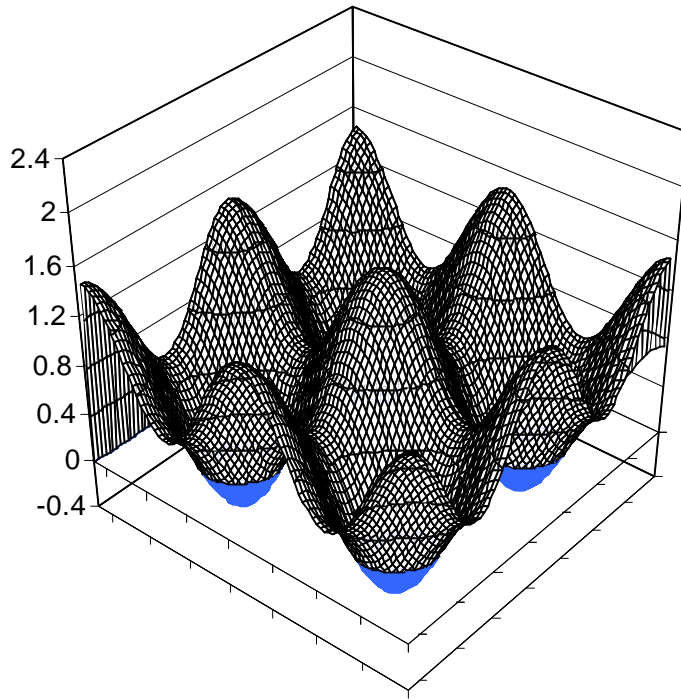


**Intensity**

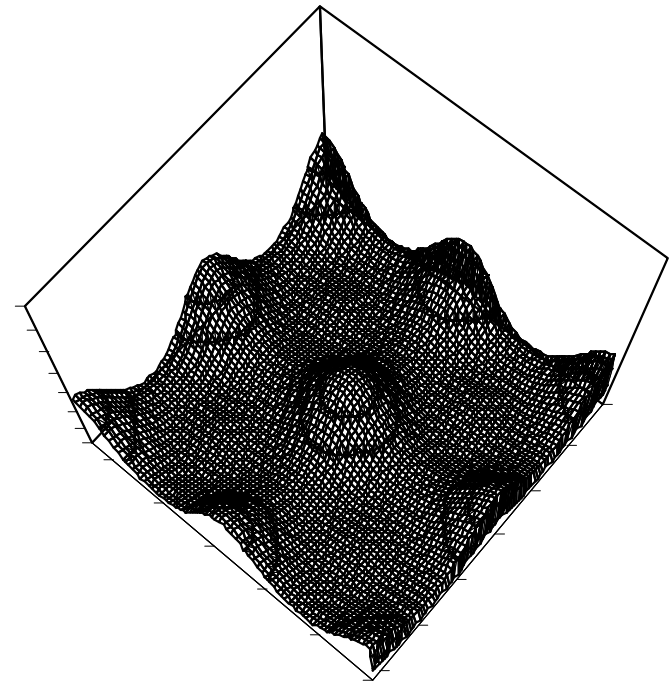
# Contacts on 2D

## X/Y Sum of Biased Cosines

1:3

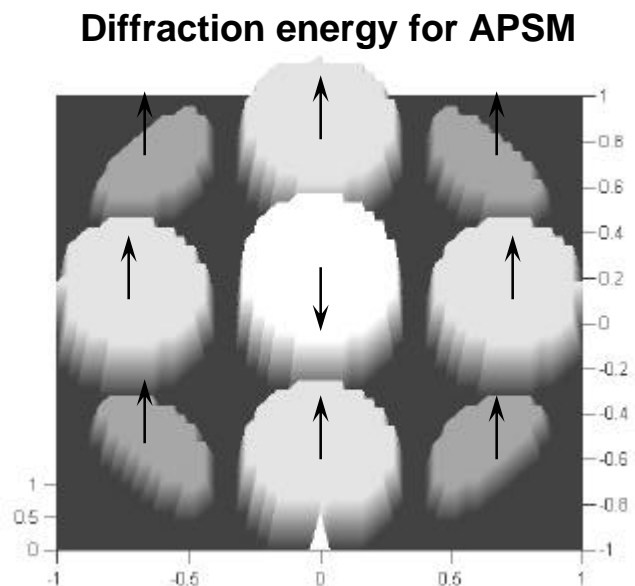
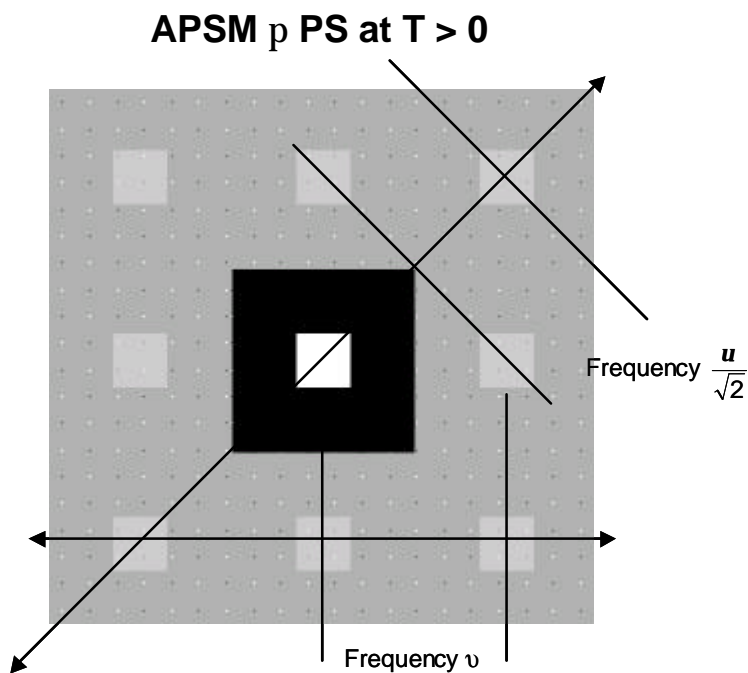


**Amplitude**



**Intensity**

# Orders for APSM



$$|\text{Mag.}|_{\text{zero order}} = [1 + \sqrt{T}](s/p) - \sqrt{T}$$

**Zero order decrease**

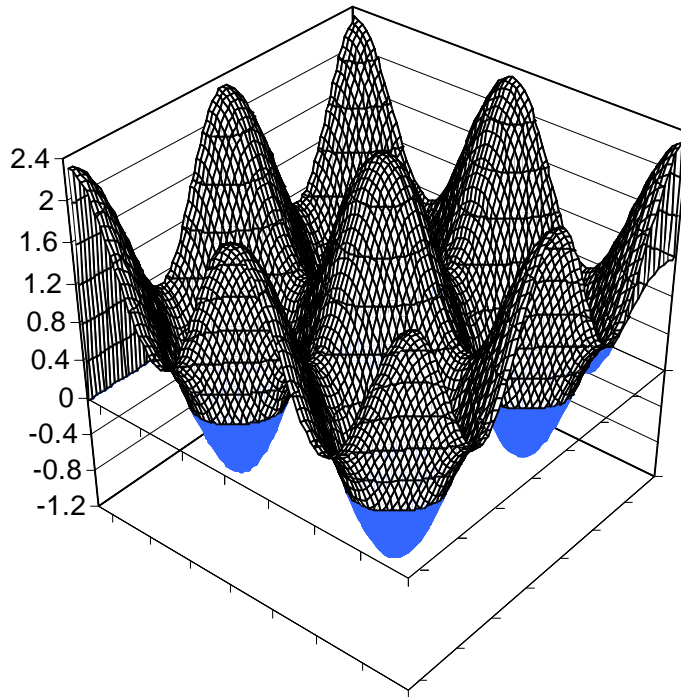
$$|\text{Mag.}|_{\text{first order}} = [1 + \sqrt{T}] \left| \left( \frac{s}{p} \right) \text{sinc} \left( \frac{s}{p} \right) \right|$$

**First order increase**

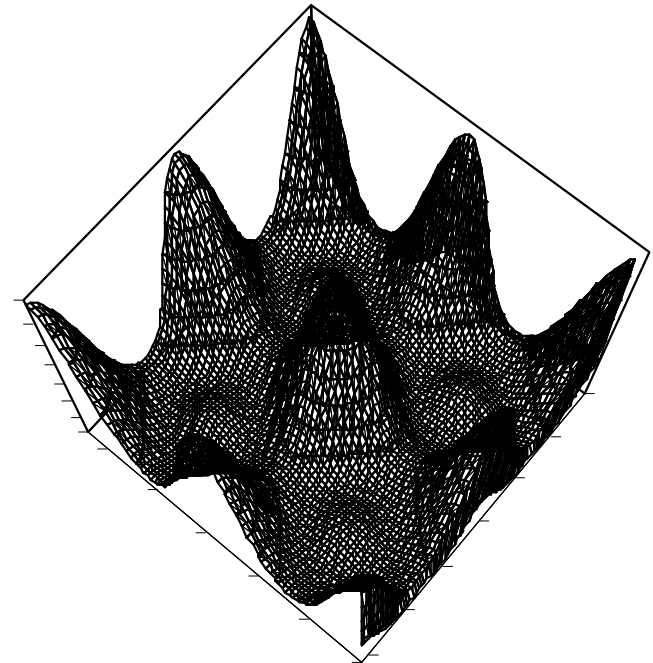
# Contacts on 2D – 6% APSM

X/Y Sum of Biased Cosines

1:1



**Amplitude**



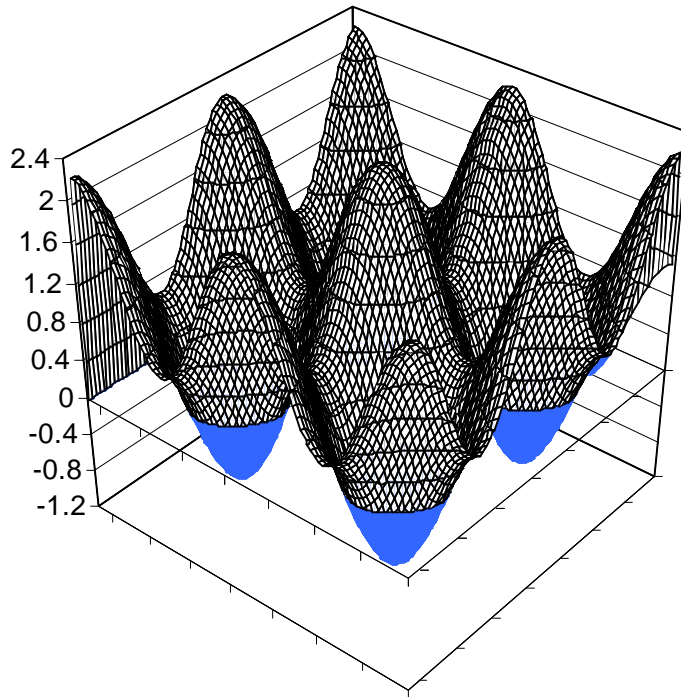
**Intensity**



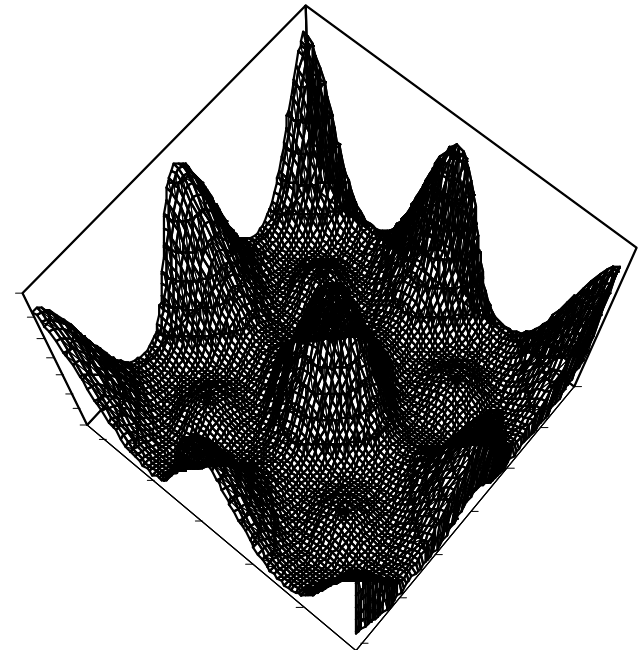
# Contacts on 2D – 6% APSM

X/Y Sum of Biased Cosines

1:1.2



**Amplitude**

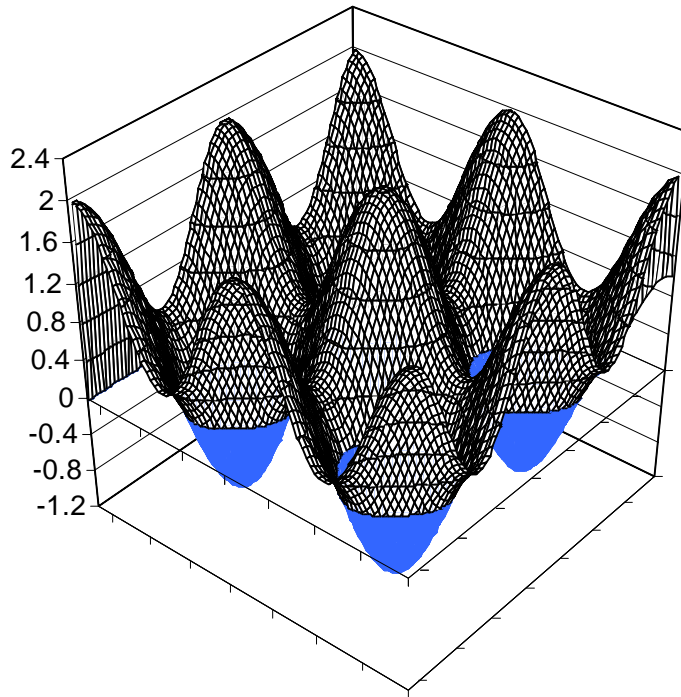


**Intensity**

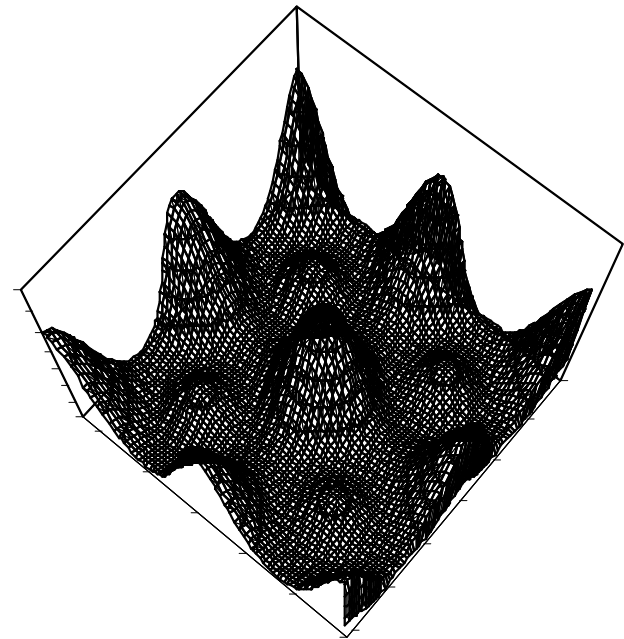
# Contacts on 2D – 6% APSM

X/Y Sum of Biased Cosines

1:1.5



**Amplitude**

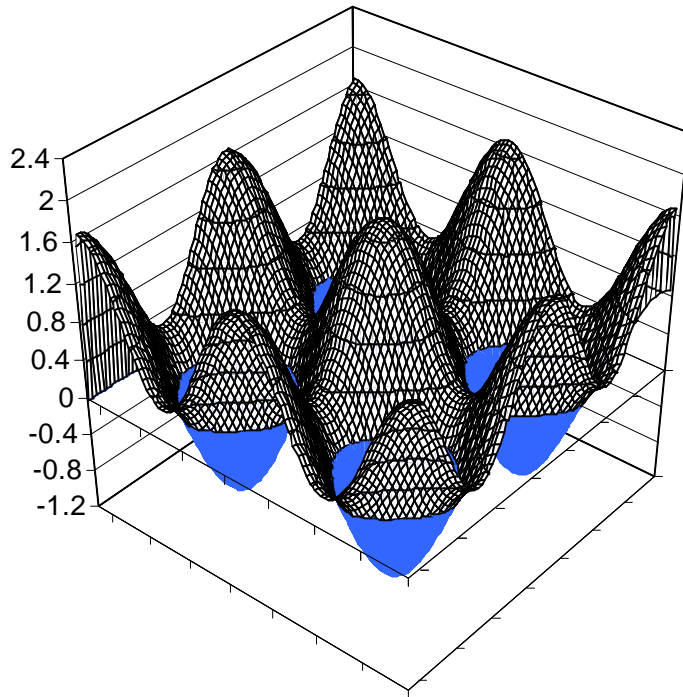


**Intensity**

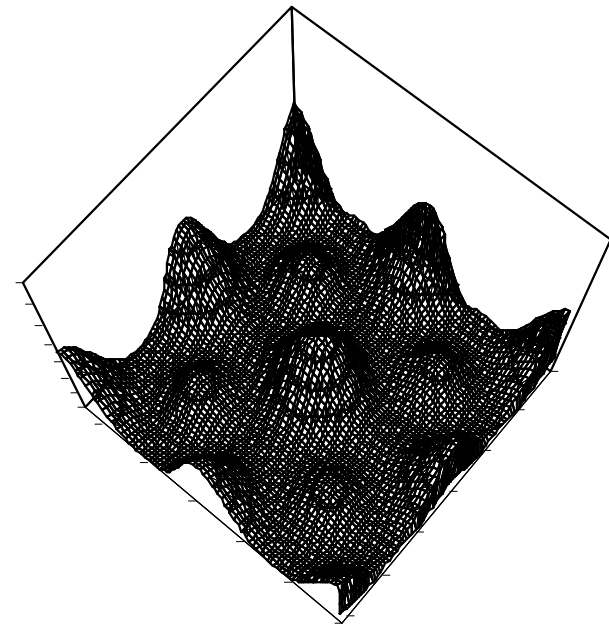
# Contacts on 2D – 6% APSM

X/Y Sum of Biased Cosines

1:2



**Amplitude**

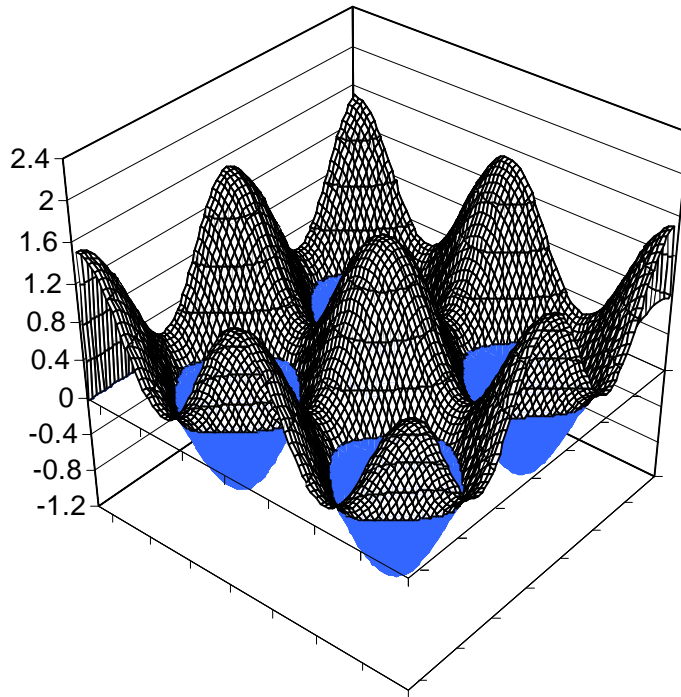


**Intensity**

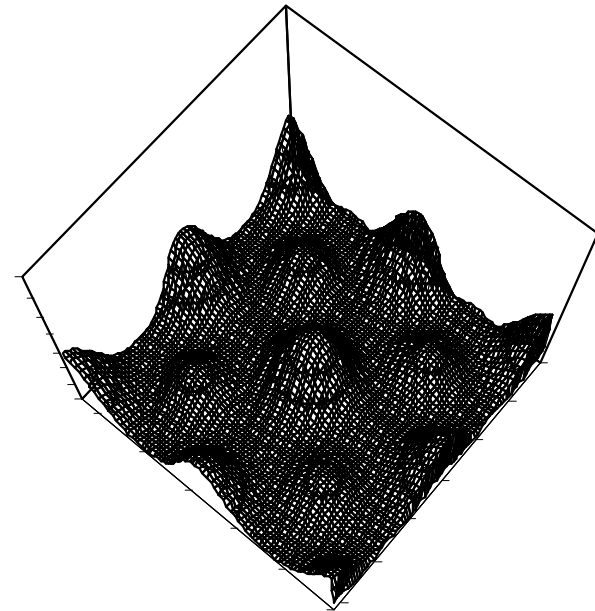
# Contacts on 2D – 6% APSM

X/Y Sum of Biased Cosines

1:2.5



**Amplitude**

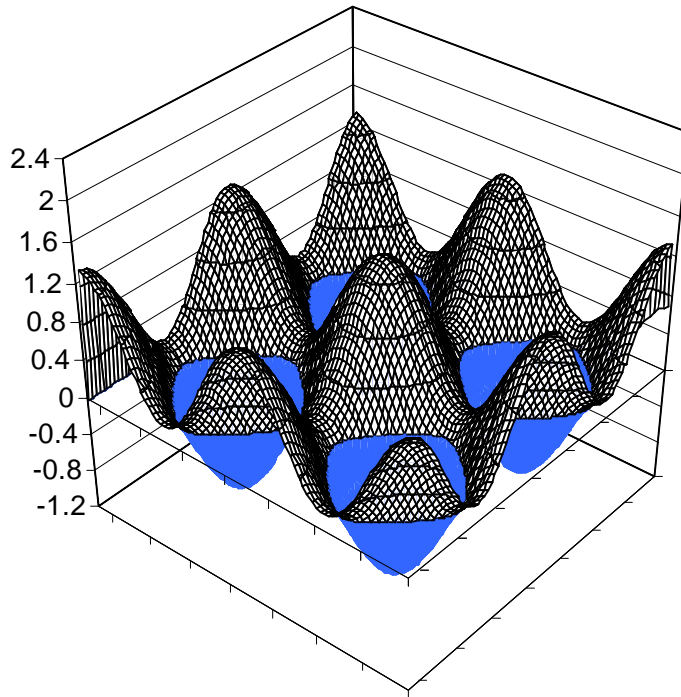


**Intensity**

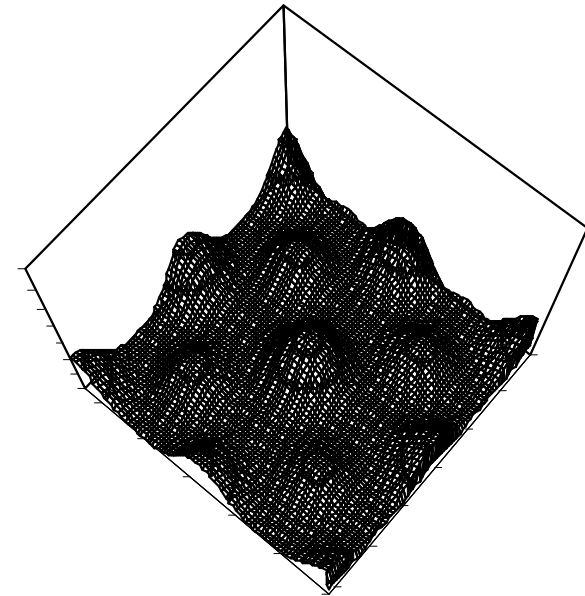
# Contacts on 2D – 6% APSM

X/Y Sum of Biased Cosines

1:3



**Amplitude**

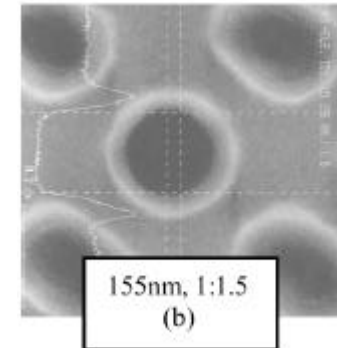
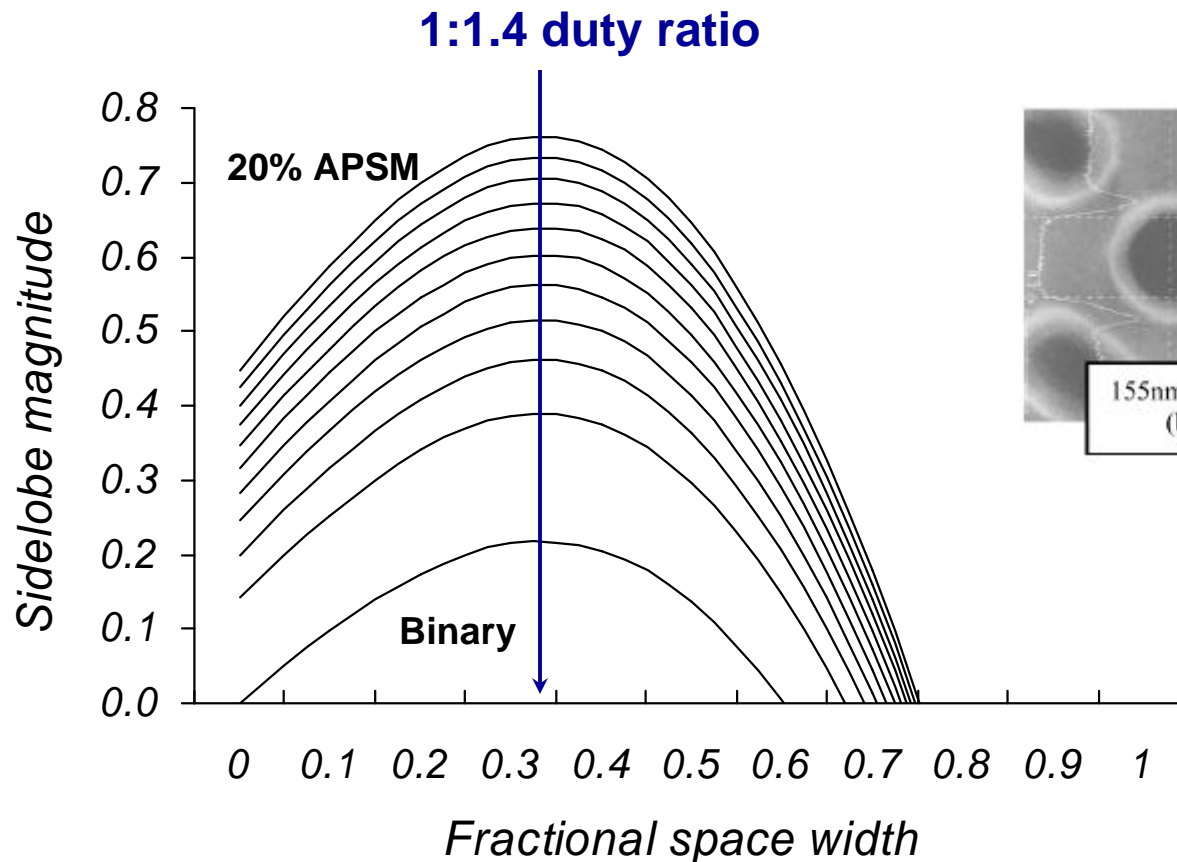


**Intensity**

# Worst Case Pitch for Sidelobes

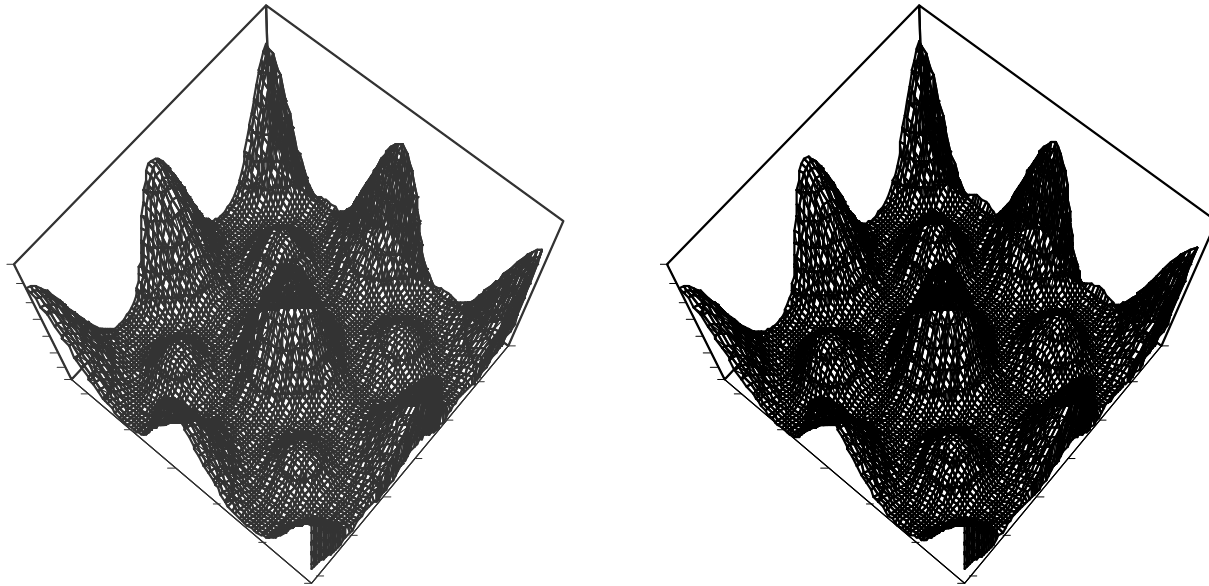
Problems when:

$$(2 \times |\text{Mag}|_{\text{first}} - |\text{Mag}|_{\text{zero}}) > \text{Resist amplitude threshold}$$



Sing et al, Proc.  
SPIE 4691.

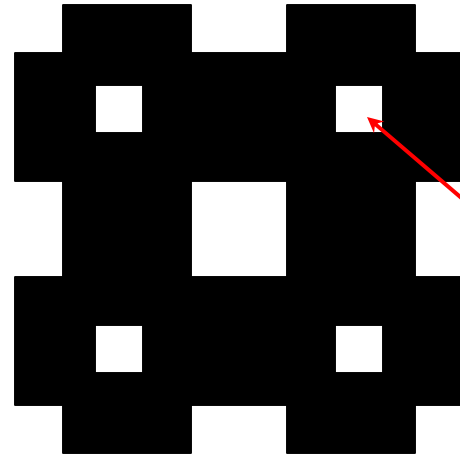
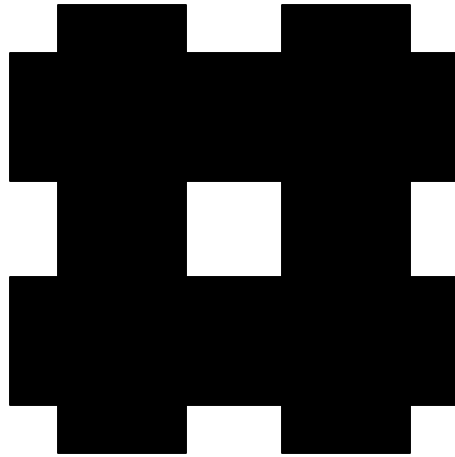
# 1:1.4 Contacts with 10% and 20% APSM



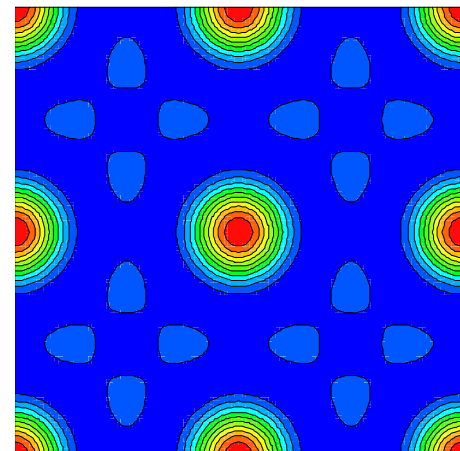
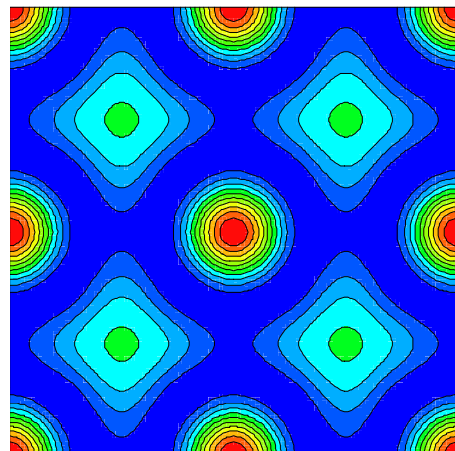
**Result of zero and first orders only.**

# Anti-sidelobe OPC

1:1.4 contacts, 10% APSM

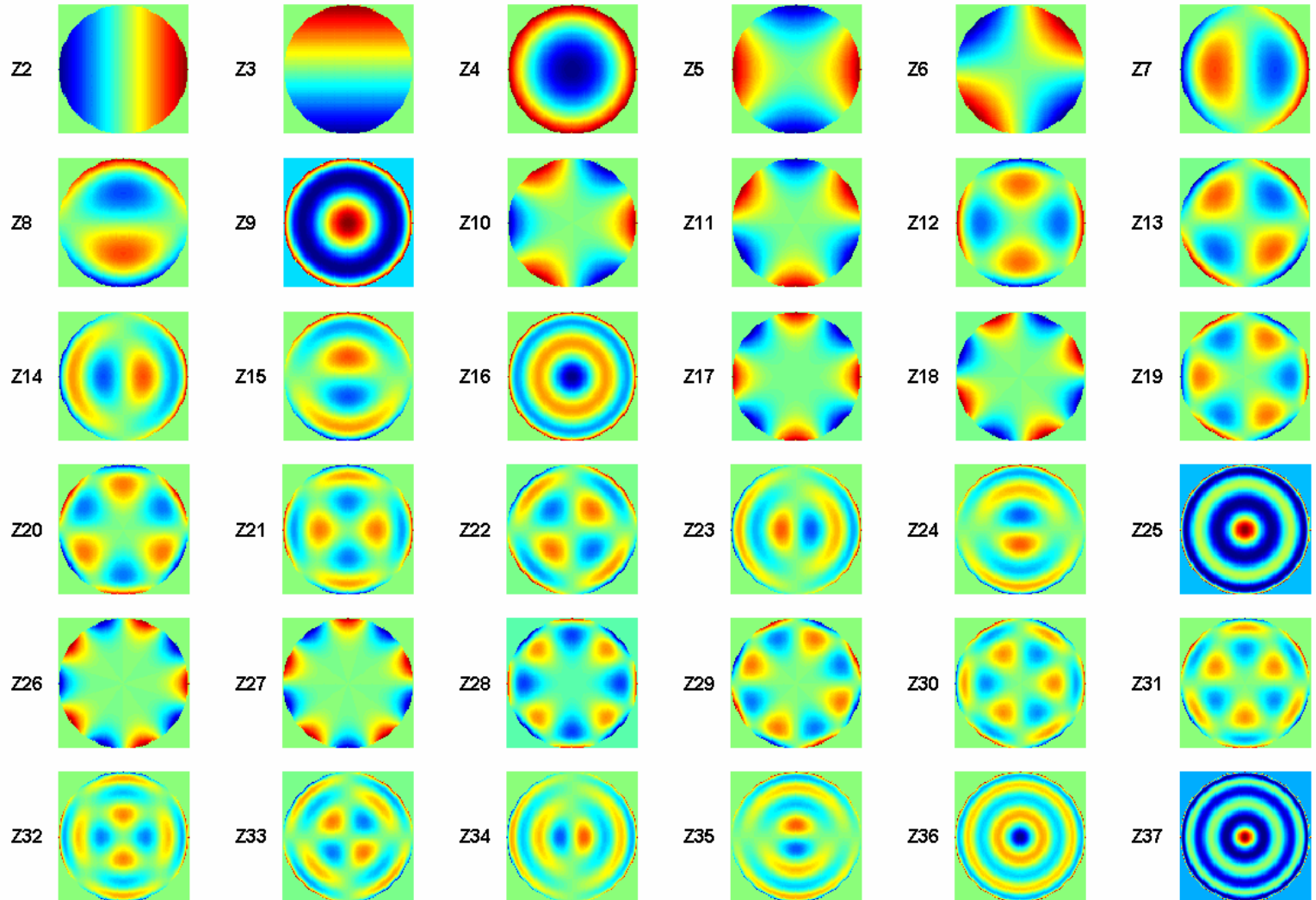


Clear anti-sidelobe

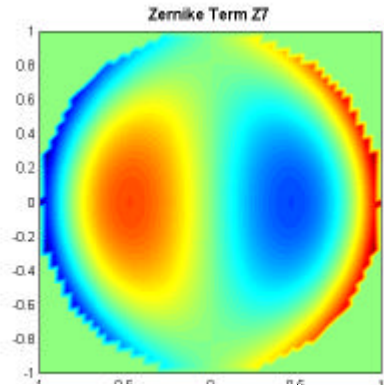




# Pitch Sensitivities to Aberration

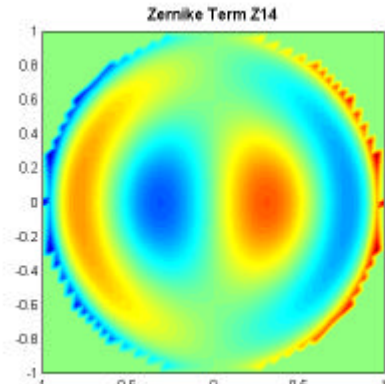


# Coma hot spots



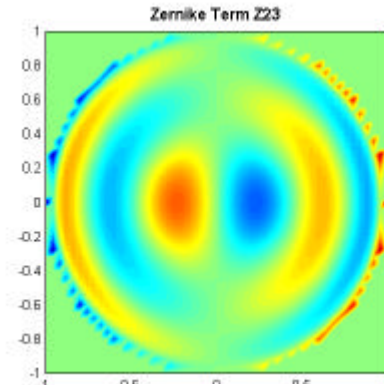
$$\left. \frac{d}{dr} \left[ (3r^3 - 2r) \cos(\theta) \right] \right| = 0$$

**Radius = +/- 0.46**



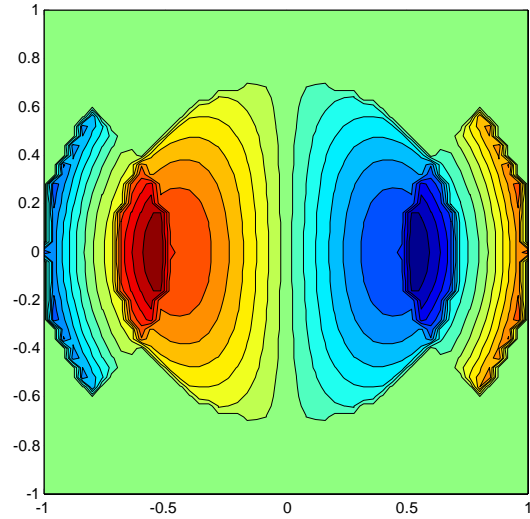
$$\left. \frac{d}{dr} \left[ (10r^5 - 12r^3 + 3r) \cdot \cos(q) \right] \right| = 0$$

**Radius = +/-0.31**

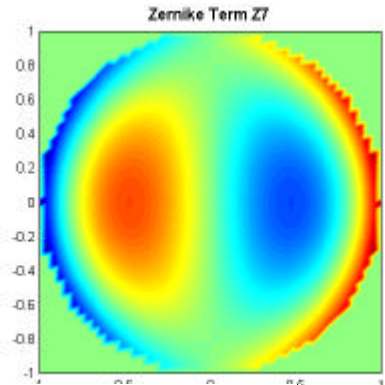


$$\left. \frac{d}{dr} \left( (35r^7 - 60r^5 + 30r^3 - 4r) \right) \right| = 0$$

**Radius = +/-0.23**

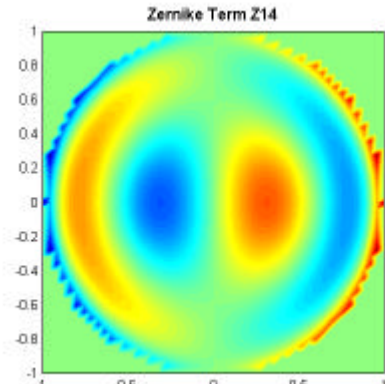


# Coma hot spots



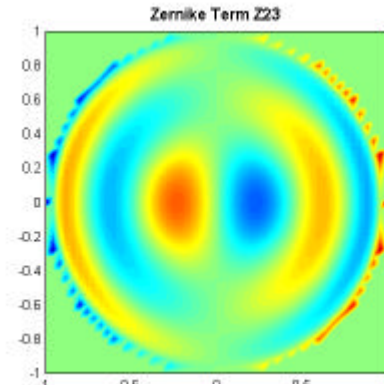
$$\left. \frac{d}{dr} \left[ (3r^3 - 2r) \cos(\theta) \right] \right| = 0$$

**Radius = +/- 0.46**



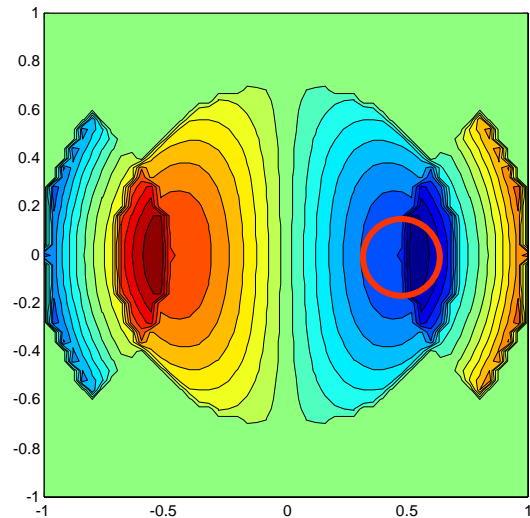
$$\left. \frac{d}{dr} \left[ (10r^5 - 12r^3 + 3r) \cdot \cos(q) \right] \right| = 0$$

**Radius = +/-0.31**

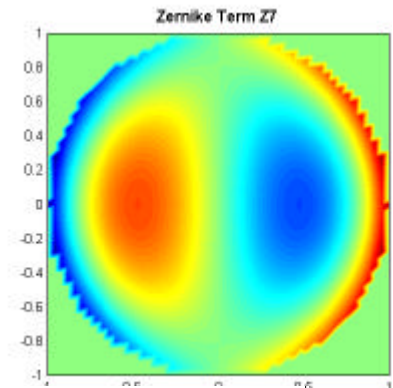


$$\left. \frac{d}{dr} \left( (35r^7 - 60r^5 + 30r^3 - 4r) \right) \right| = 0$$

**Radius = +/-0.23**

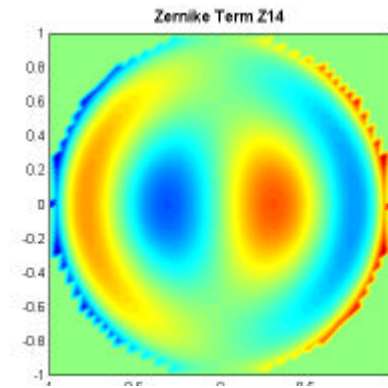


# Coma hot spots



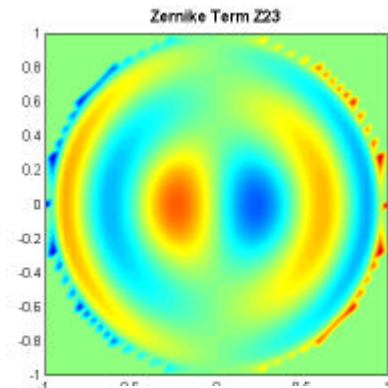
$$\left. \frac{d}{dr} \left[ (3r^3 - 2r) \cos(\theta) \right] \right| = 0$$

**Radius = +/- 0.46**



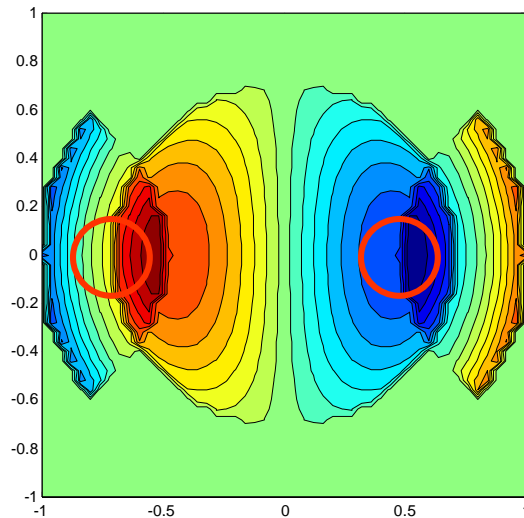
$$\left. \frac{d}{dr} \left[ (10r^5 - 12r^3 + 3r) \cdot \cos(q) \right] \right| = 0$$

**Radius = +/-0.31**

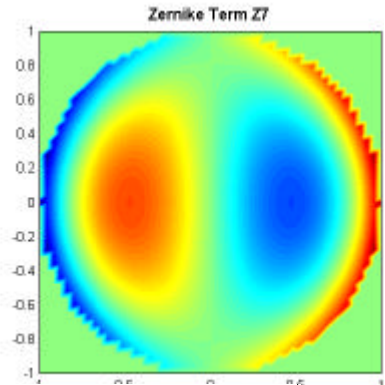


$$\left. \frac{d}{dr} \left( (35r^7 - 60r^5 + 30r^3 - 4r) \right) \right| = 0$$

**Radius = +/-0.23**

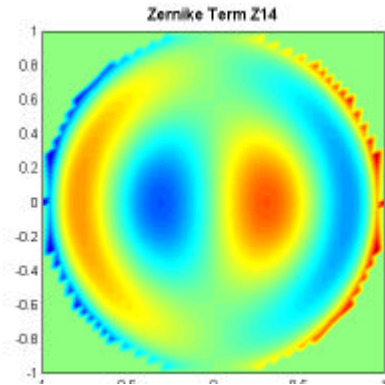


# Coma hot spots



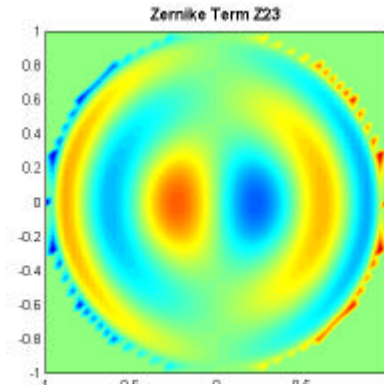
$$\left. \frac{d}{dr} \left[ (3r^3 - 2r) \cos(\theta) \right] \right| = 0$$

Radius = +/- 0.46



$$\left. \frac{d}{dr} \left[ (10r^5 - 12r^3 + 3r) \cdot \cos(q) \right] \right| = 0$$

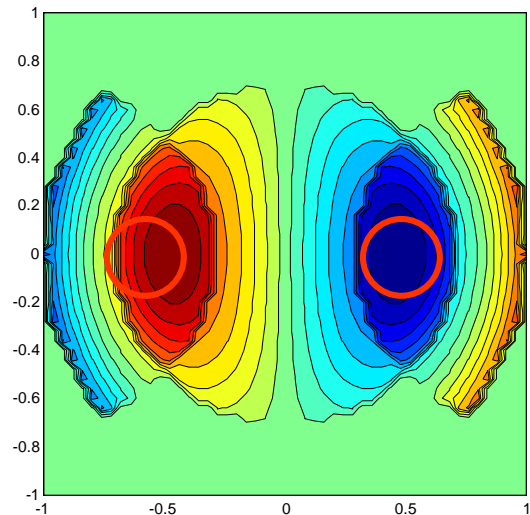
Radius = +/- 0.31



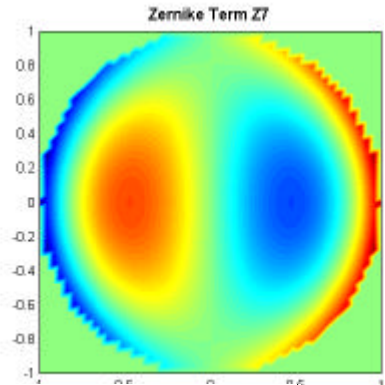
$$\left. \frac{d}{dr} \left( (35r^7 - 60r^5 + 30r^3 - 4r) \right) \right| = 0$$

Radius = +/- 0.23

Increasing Pitch

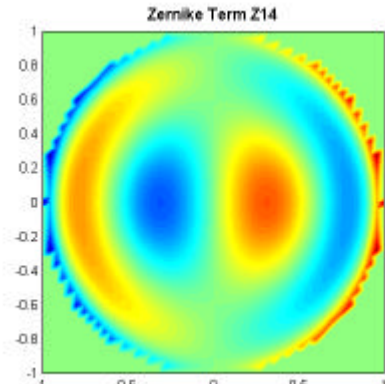


# Coma hot spots



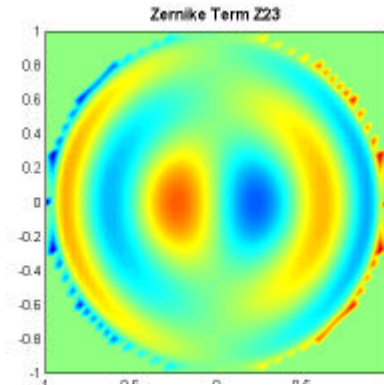
$$\left. \frac{d}{dr} \left[ (3r^3 - 2r) \cos(\theta) \right] \right| = 0$$

Radius = +/- 0.46



$$\left. \frac{d}{dr} \left[ (10r^5 - 12r^3 + 3r) \cdot \cos(q) \right] \right| = 0$$

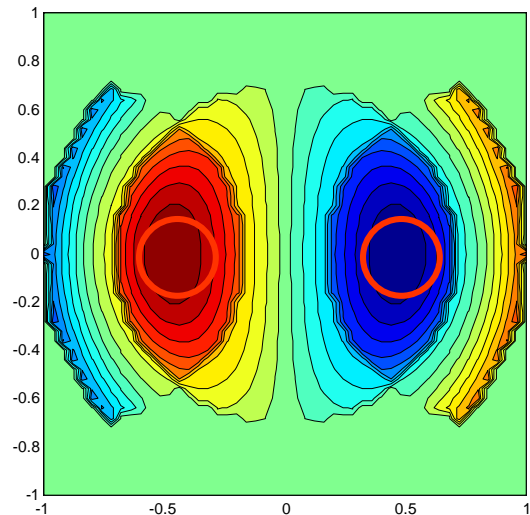
Radius = +/- 0.31



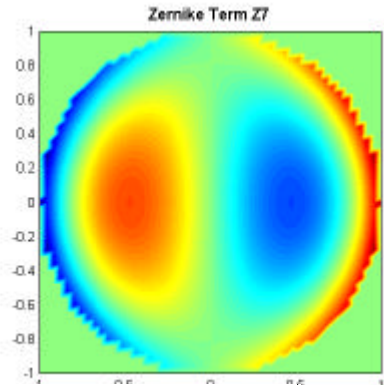
$$\left. \frac{d}{dr} \left( (35r^7 - 60r^5 + 30r^3 - 4r) \right) \right| = 0$$

Radius = +/- 0.23

Increasing Pitch

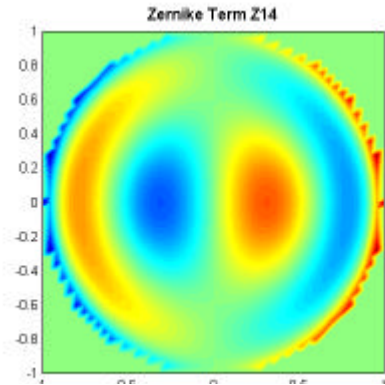


# Coma hot spots



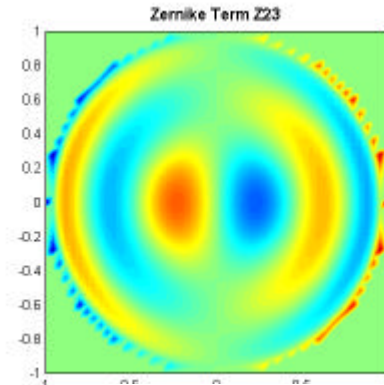
$$\left. \frac{d}{dr} \left[ (3r^3 - 2r) \cos(\theta) \right] \right| = 0$$

Radius = +/- 0.46



$$\left. \frac{d}{dr} \left[ (10r^5 - 12r^3 + 3r) \cdot \cos(q) \right] \right| = 0$$

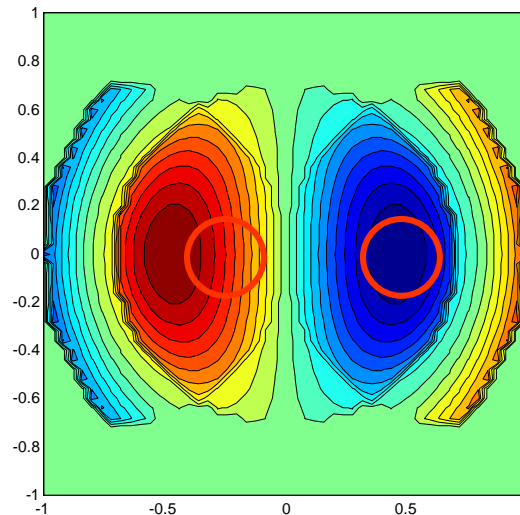
Radius = +/- 0.31



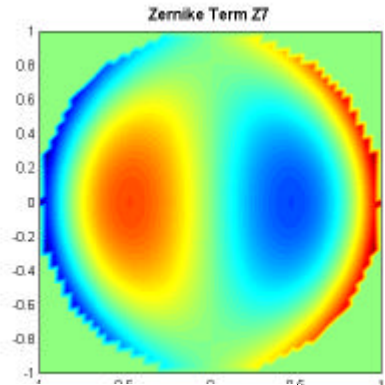
$$\left. \frac{d}{dr} \left( (35r^7 - 60r^5 + 30r^3 - 4r) \right) \right| = 0$$

Radius = +/- 0.23

Increasing  
Pitch

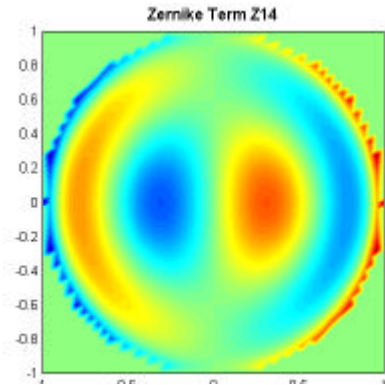


# Coma hot spots



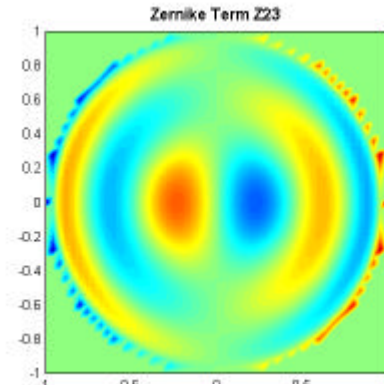
$$\left. \frac{d}{dr} \left[ (3r^3 - 2r) \cos(\theta) \right] \right| = 0$$

Radius = +/- 0.46



$$\left. \frac{d}{dr} \left[ (10r^5 - 12r^3 + 3r) \cdot \cos(q) \right] \right| = 0$$

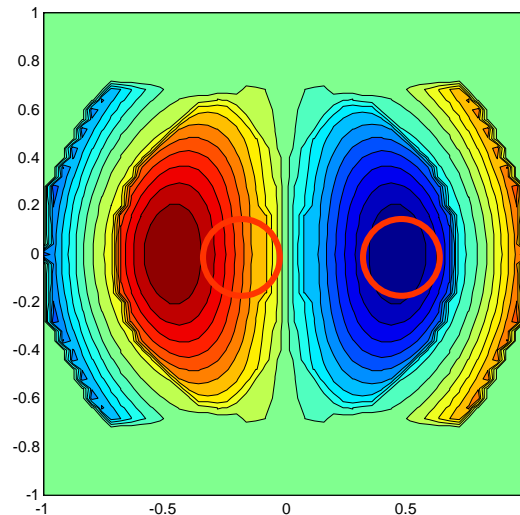
Radius = +/- 0.31



$$\left. \frac{d}{dr} \left( (35r^7 - 60r^5 + 30r^3 - 4r) \right) \right| = 0$$

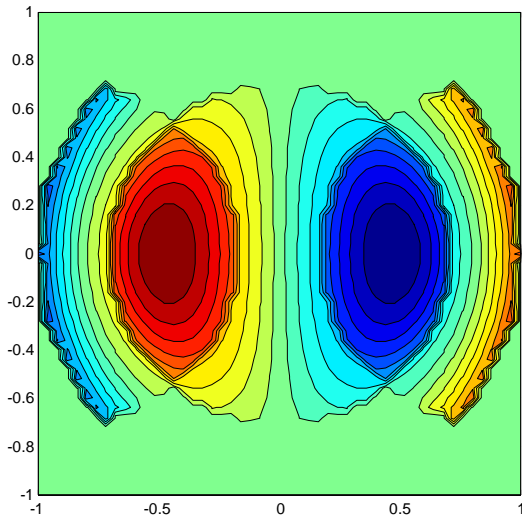
Radius = +/- 0.23

Increasing Pitch



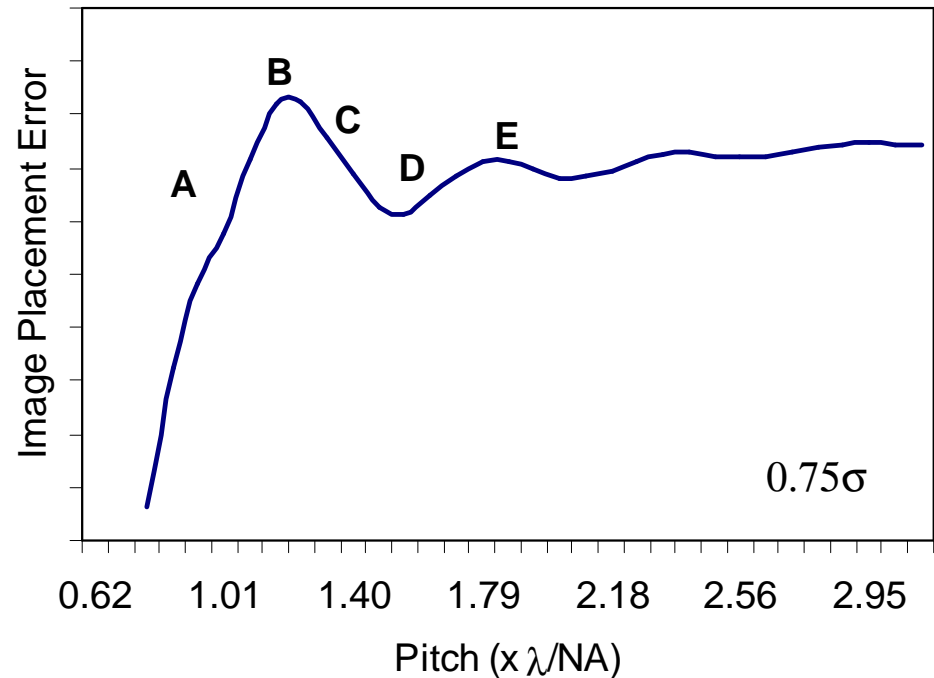


# Image Placement Error with Coma



**Dominant Effect**

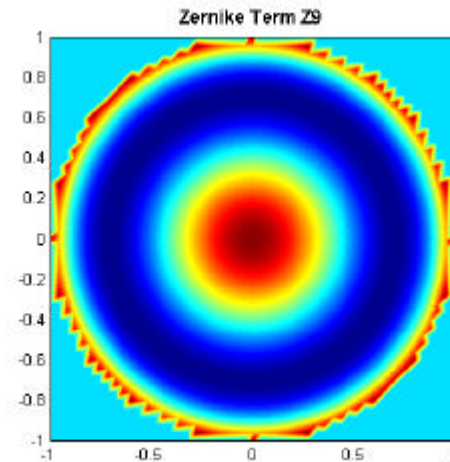
- A - 1<sup>st</sup> order to coma max
- B - 1<sup>st</sup> order at coma max
- C - 1<sup>st</sup> order to center
- D - 2<sup>nd</sup> order to coma max
- E - 2<sup>nd</sup> order at coma max



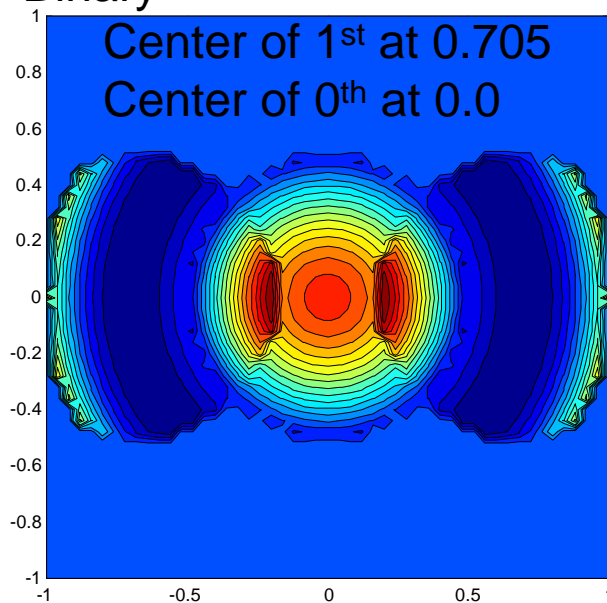
# Spherical hot spots

$$\frac{d}{dr} \left[ (6 \cdot r^4 - 6 \cdot r^2) + 1 \right] = 0$$

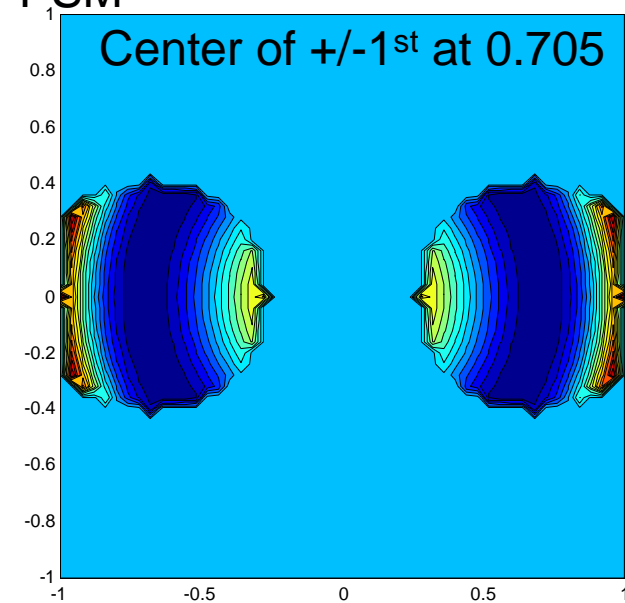
**Radius = 0.705**



Binary



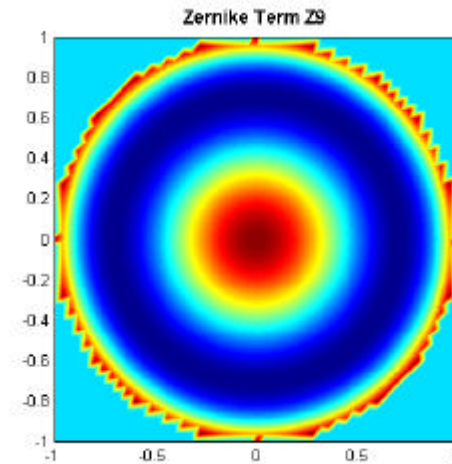
PSM



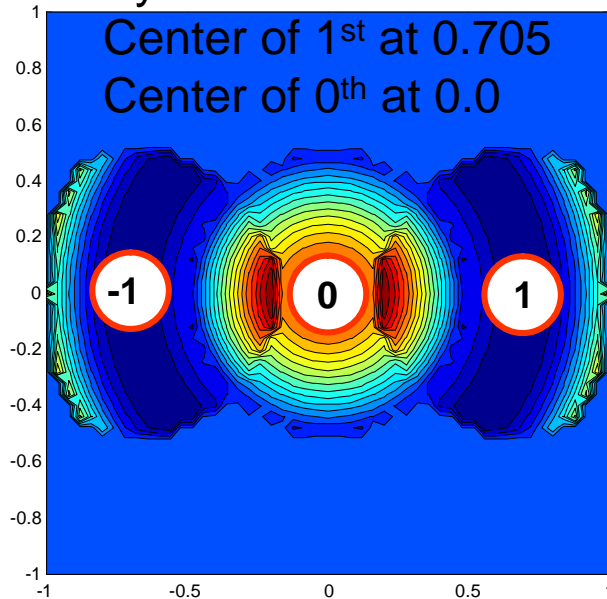
# Spherical hot spots

$$\frac{d}{dr} \left[ (6 \cdot r^4 - 6 \cdot r^2) + 1 \right] = 0$$

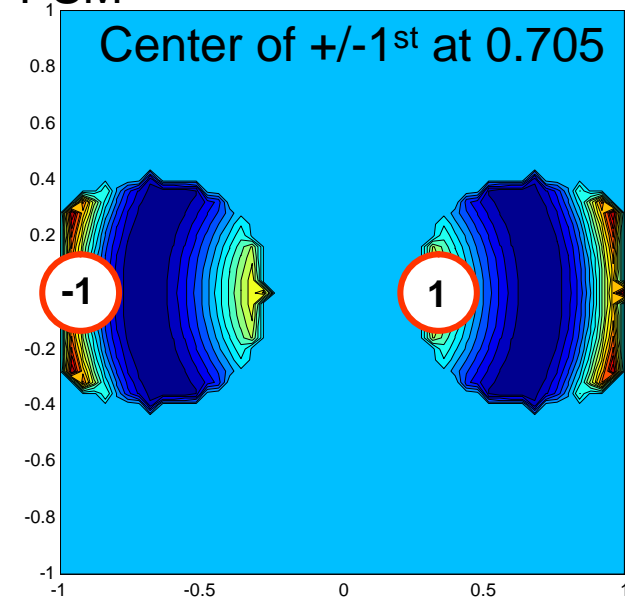
Radius = 0.705



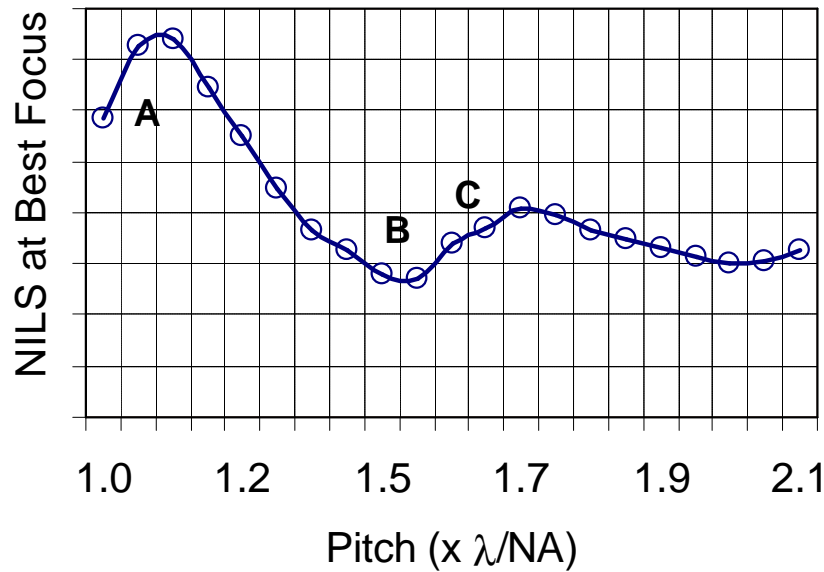
Binary



PSM



# Spherical hot spots



## Dominant Effect

A – 1<sup>st</sup> order collection

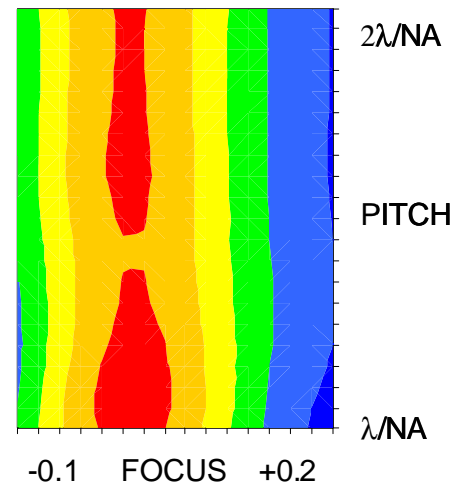
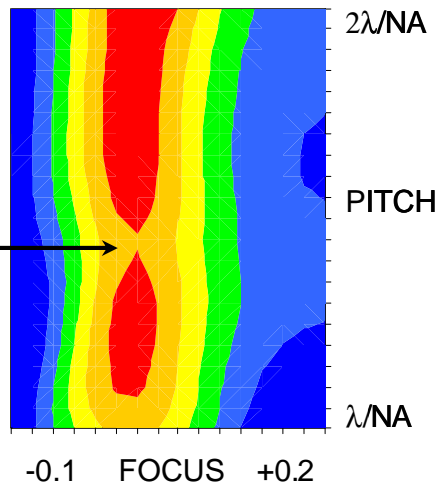
B - 1<sup>st</sup> order at spherical max

C – 2<sup>nd</sup> order collection

0.5 sigma

0.9 sigma

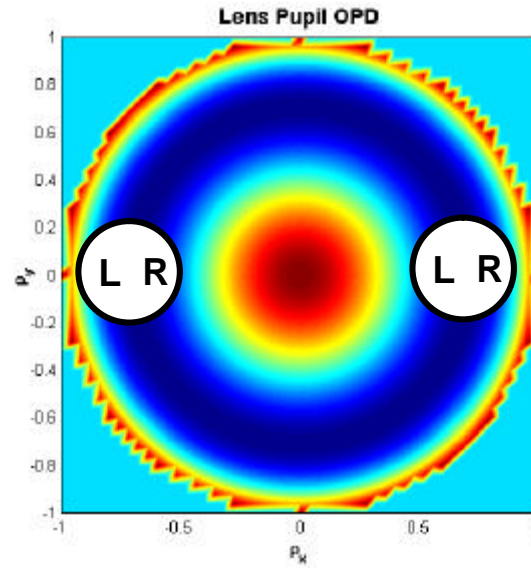
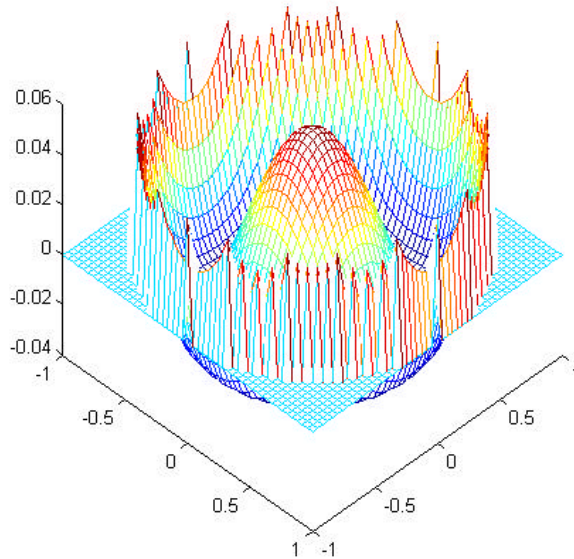
Radius = 0.705



# Summary

- Binary pitch follows  $\frac{ml}{(S \pm 1)NA}$
- OAI pitch follows  $\frac{ml}{R(S_c + S_r + 1)NA}$
- Assist features have pitch and (bar + space) sensitivity
- Contact side-lobes are a primary order effect
- Aberration sensitivity follows derivative of aberration

# Phase Shift Mask and Spherical



ALT PSM,  
0.85NA, 0.2W  
spherical

0.2 sigma

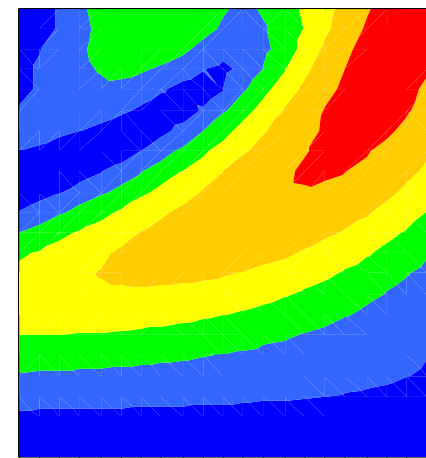
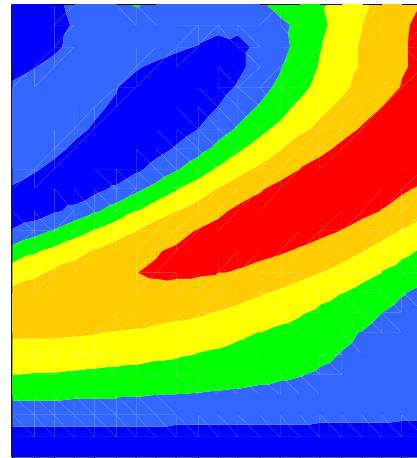
0.4 sigma

0.6 sigma

$1.5\lambda/\text{NA}$

PITCH

$0.5\lambda/\text{NA}$



$1.5\lambda/\text{NA}$

PITCH

$0.5\lambda/\text{NA}$

-0.3 FOCUS +0.1

-0.3 FOCUS +0.1

-0.3 FOCUS +0.1